
CS688: Web-Scale Image Search
Scale Invariant Region Selection and
SIFT

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Course URL:

<http://sgvr.kaist.ac.kr/~sungeui/IR>

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Announcements

- **Parts of my book are updated**
- **One of students is invited to each class**

Class Objectives (Ch. 2.4)

- **Scale invariant region selection**
 - **Automatic scale selection**
 - **Laplacian of Gradients (LoG) \approx Difference of Gradients (DoG)**
 - **SIFT as a local descriptor**

- **At last time, we discussed:**
 - **Different conferences**
 - **Image descriptors that are invariant to various changes**
 - **Harris corner detector**

From Points to Regions...

- The Harris and Hessian operators define interest points.
 - Precise localization
 - High repeatability

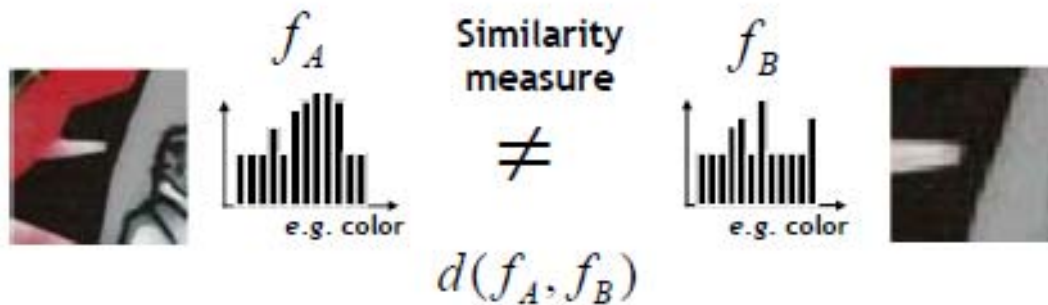


- In order to compare those points, we need to compute a descriptor over a region.
 - How can we define such a region in a scale invariant manner?
- *I.e. how can we detect scale invariant interest regions?*

Source: Bastian Leibe

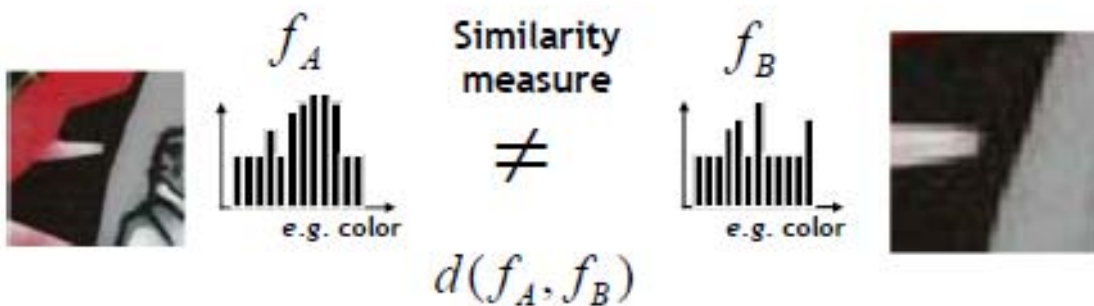
Naïve Approach: Exhaustive Search

- Multi-scale procedure
 - Compare descriptors while varying the patch size



Naïve Approach: Exhaustive Search

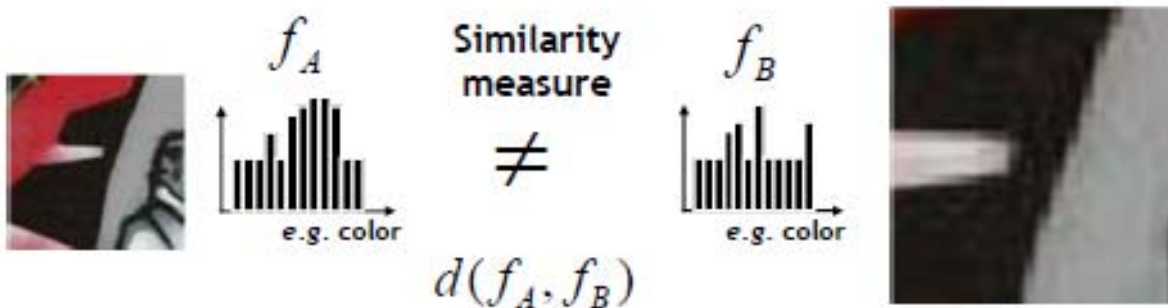
- Multi-scale procedure
 - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

Naïve Approach: Exhaustive Search

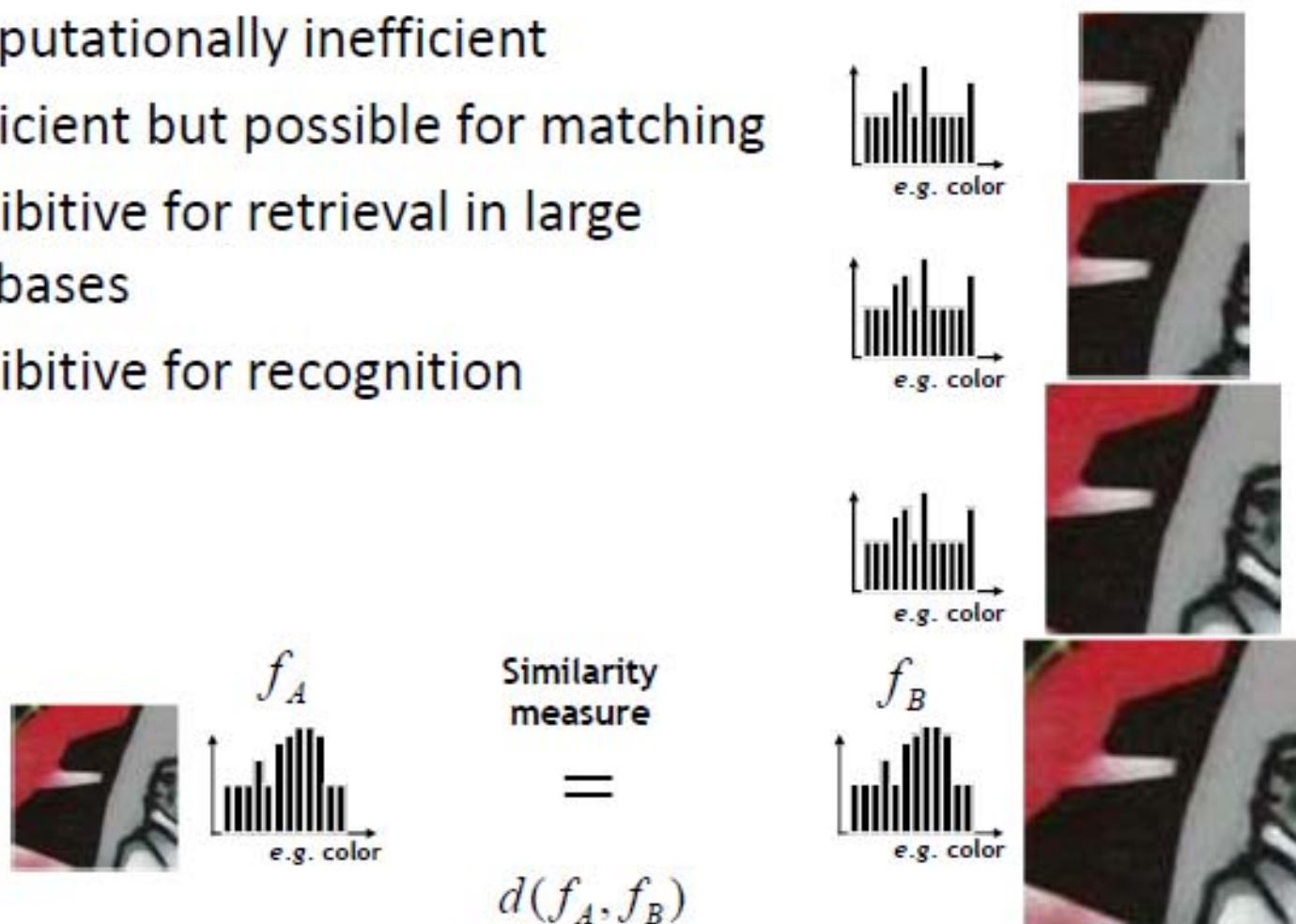
- Multi-scale procedure
 - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

Naïve Approach: Exhaustive Search

- Comparing descriptors while varying the patch size
 - Computationally inefficient
 - Inefficient but possible for matching
 - Prohibitive for retrieval in large databases
 - Prohibitive for recognition



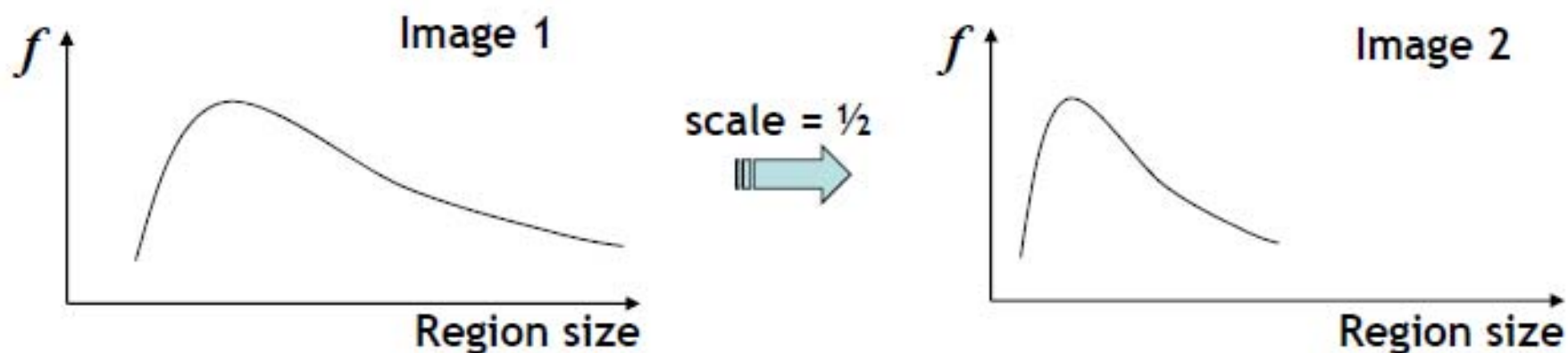
Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

- Solution:
 - Design a function on the region, which is “scale invariant”
(*the same for corresponding regions, even if they are at different scales*)

Example: average intensity. For corresponding regions (even of different sizes) it will be the same.

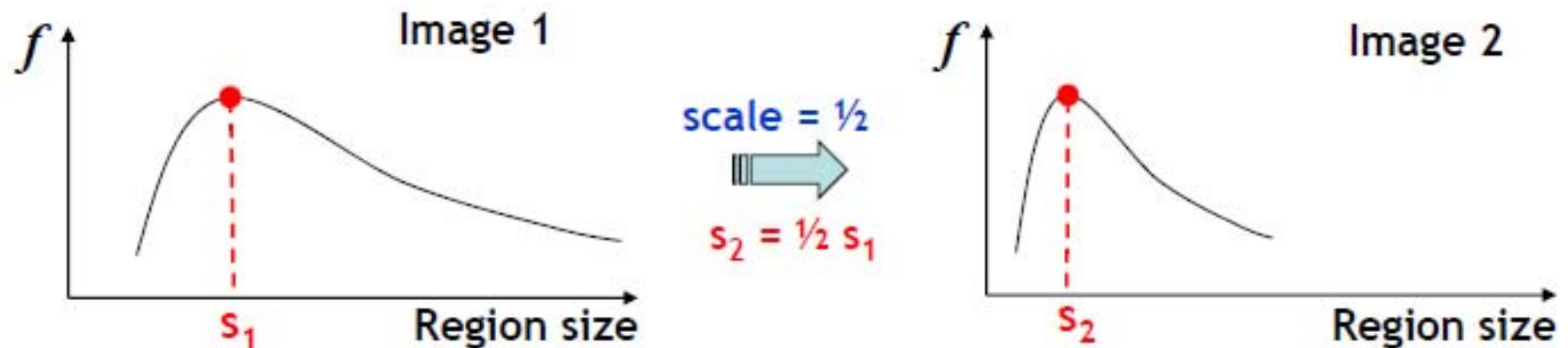
- For a point in one image, we can consider it as a function of region size (patch width)



Slide credit: Kristen Grauman

Automatic Scale Selection

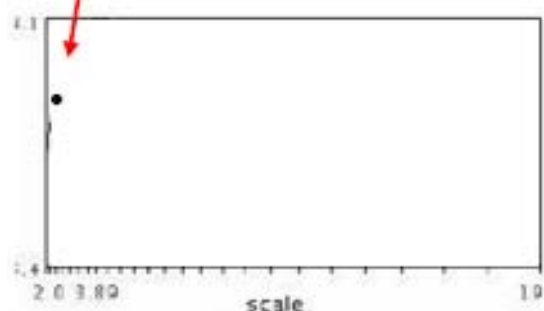
- Common approach:
 - Take a local maximum of this function.
 - Observation: region size for which the maximum is achieved should be *invariant* to image scale.



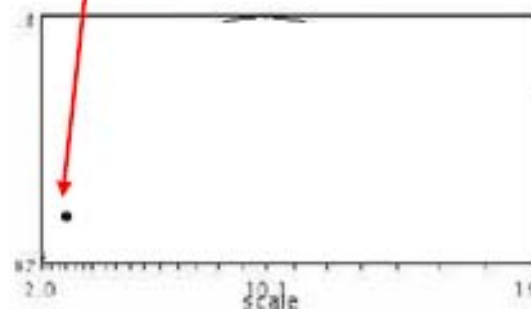
Slide credit: Kristen Grauman

Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1 \dots i_m}(x, \sigma))$$

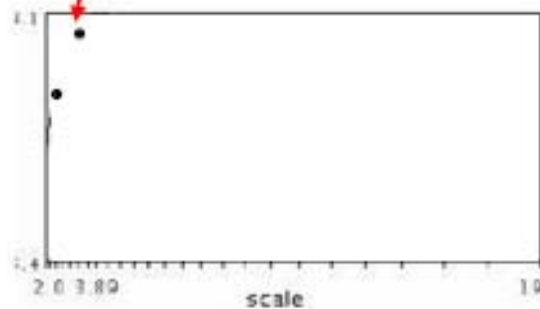


$$f(I_{i_1 \dots i_m}(x', \sigma))$$

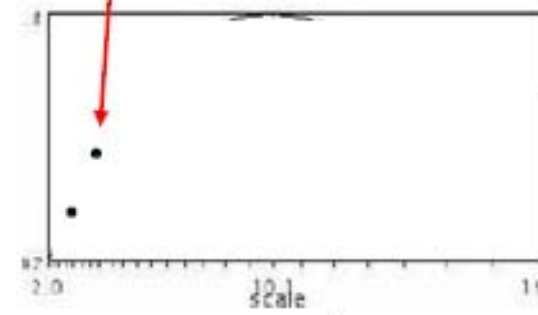
Slide credit: Krystian Mikolajczyk

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$$f(I_{i_1...i_m}(x, \sigma))$$

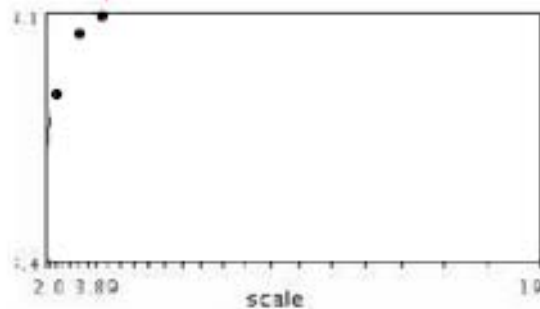


$$f(I_{i_1...i_m}(x', \sigma))$$

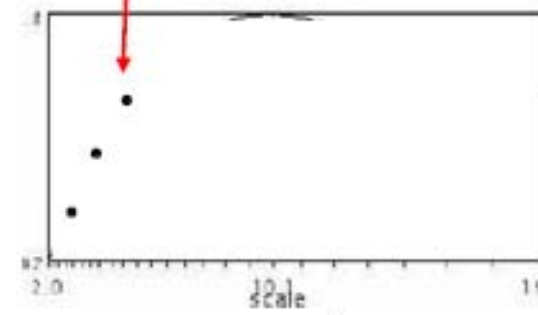
Slide credit: Krystian Mikolajczyk

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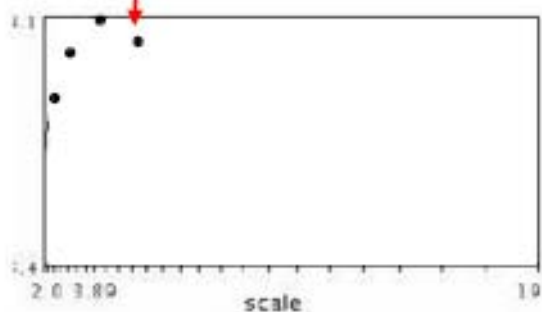


$$f(I_{i_1...i_m}(x', \sigma))$$

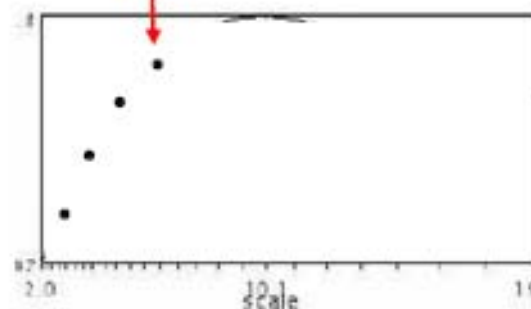
Slide credit: Krystian Mikolajczyk

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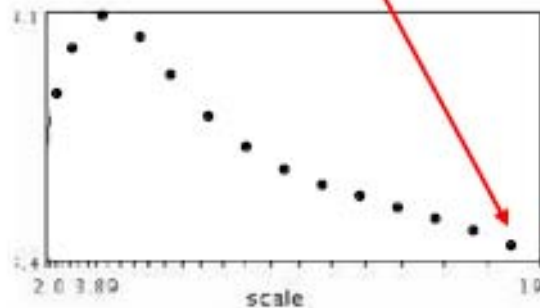


$$f(I_{i_1...i_m}(x', \sigma))$$

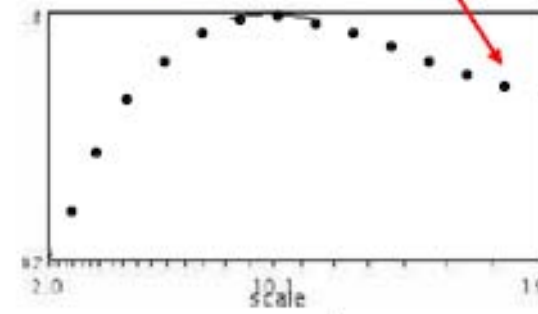
Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1...i_m}(x, \sigma))$$

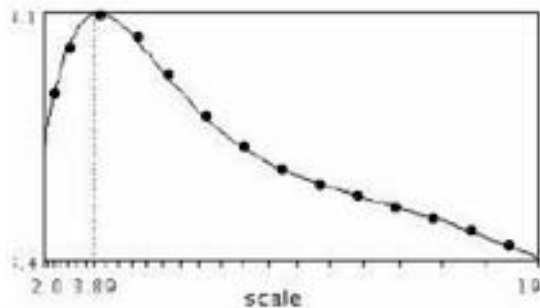


$$f(I_{i_1...i_m}(x', \sigma))$$

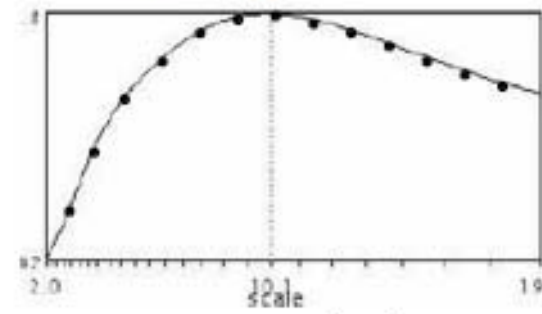
Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1 \dots i_m}(x, \sigma))$$

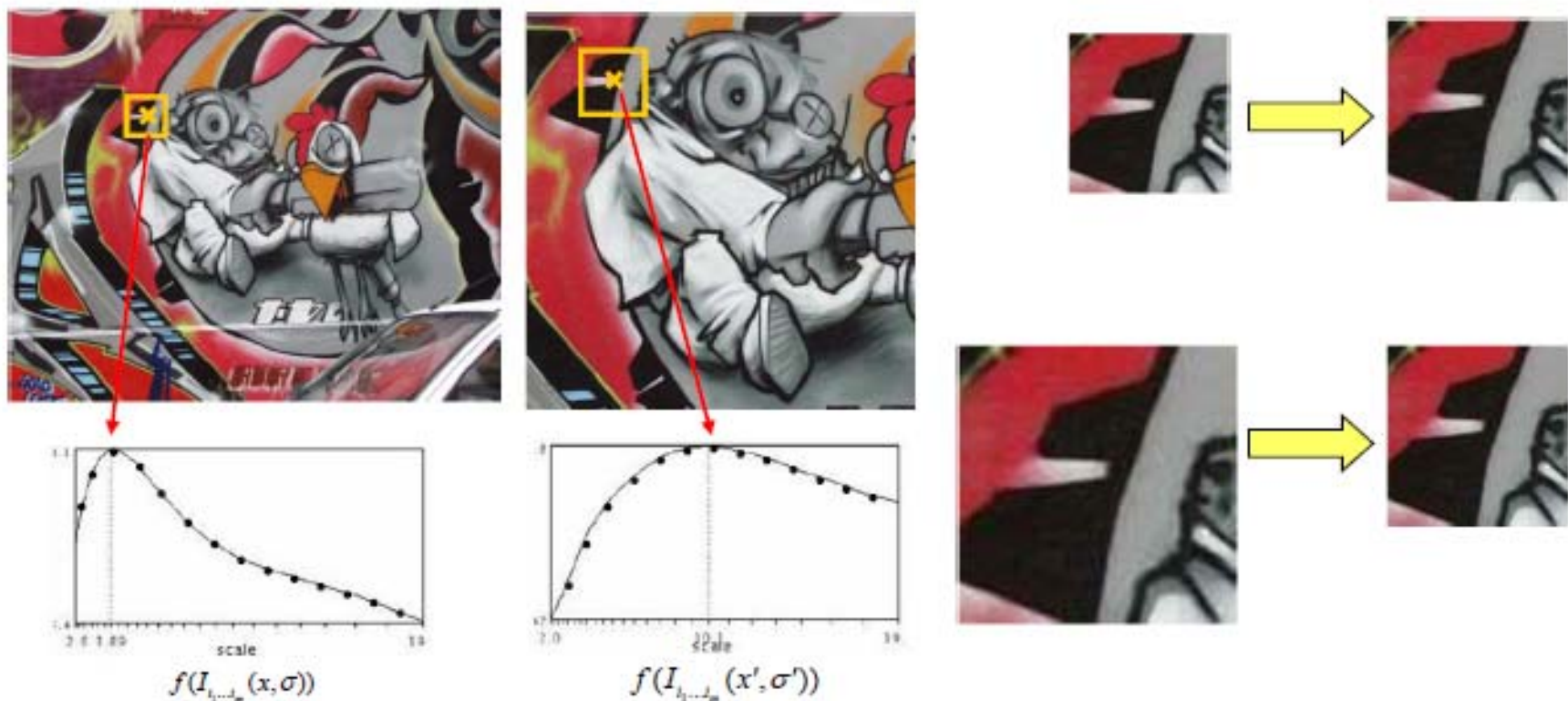


$$f(I_{i_1 \dots i_m}(x', \sigma'))$$

Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

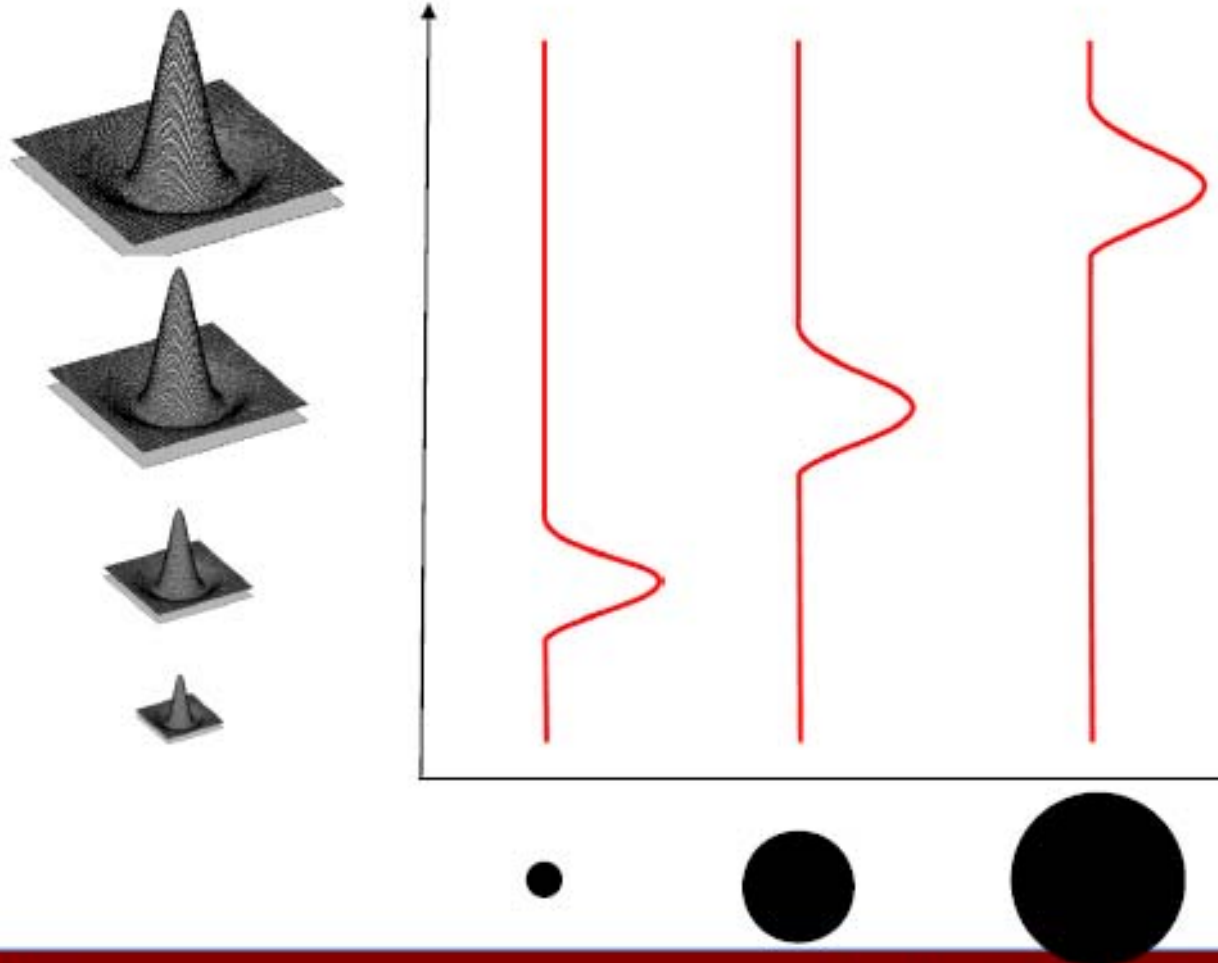
- Normalize: Rescale to fixed size



Slide credit: Tinne Tuytelaars

What Is A Useful Signature Function?

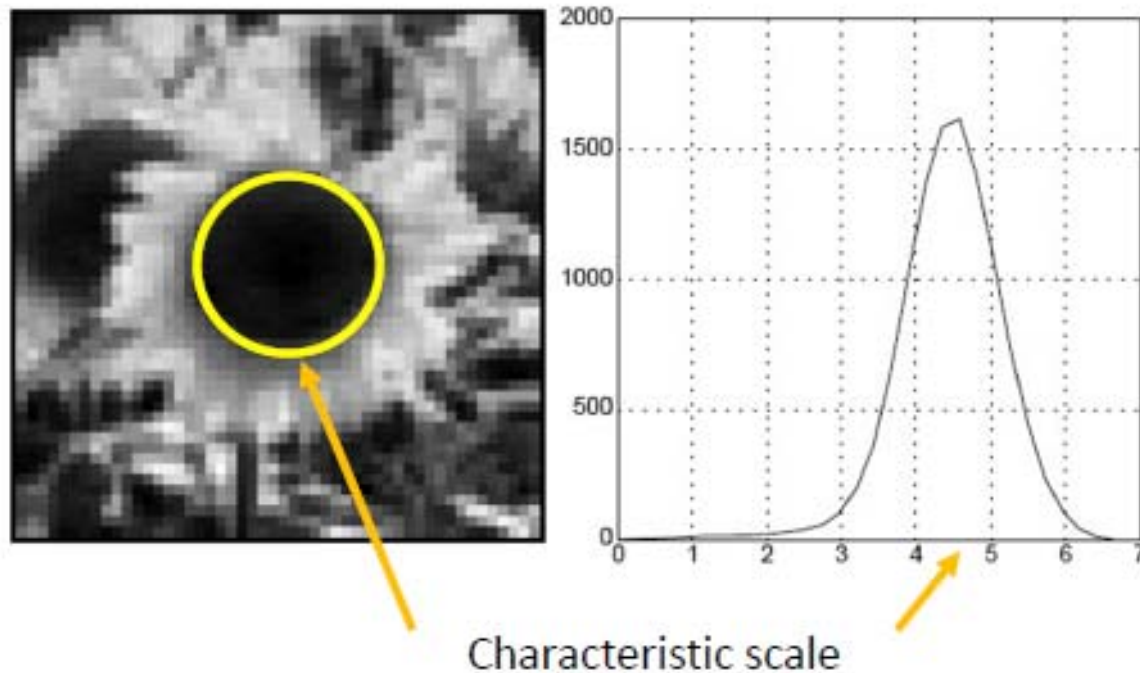
- Laplacian-of-Gaussian = “blob” detector



Slide credit: Bastian Leibe

Characteristic Scale

- We define the *characteristic scale* as the scale that produces peak of Laplacian response

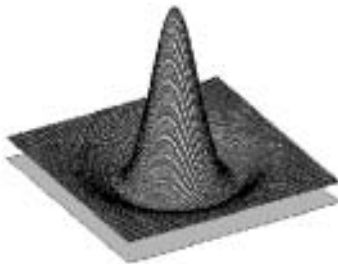


T. Lindeberg (1998). ["Feature detection with automatic scale selection."](#) *International Journal of Computer Vision* 30 (2): pp 77–116.

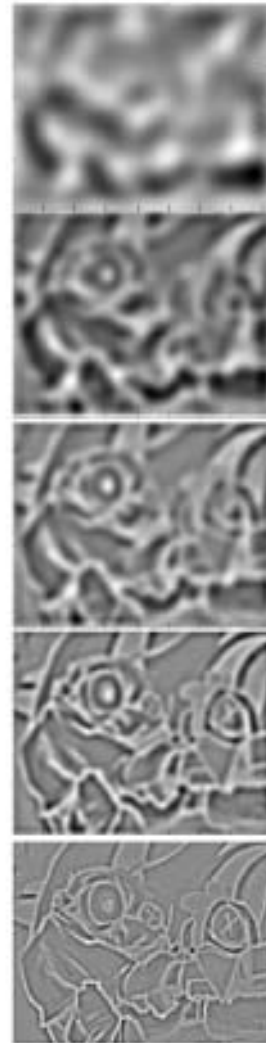
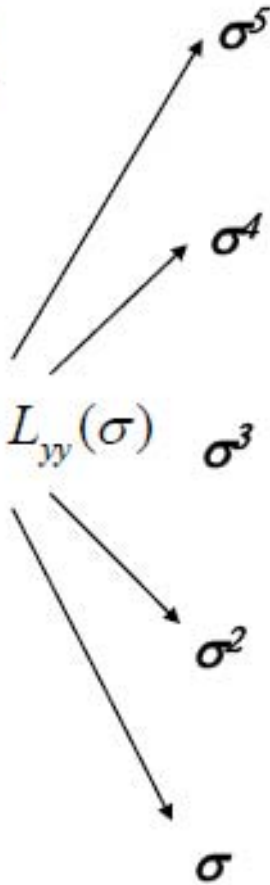
Slide credit: Svetlana Lazebnik

Laplacian-of-Gaussian (LoG)

- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



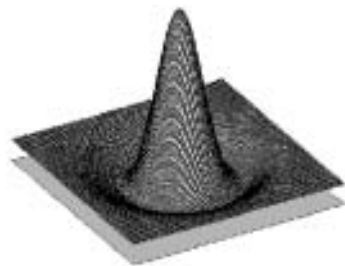
$$L_{xx}(\sigma) + L_{yy}(\sigma)$$



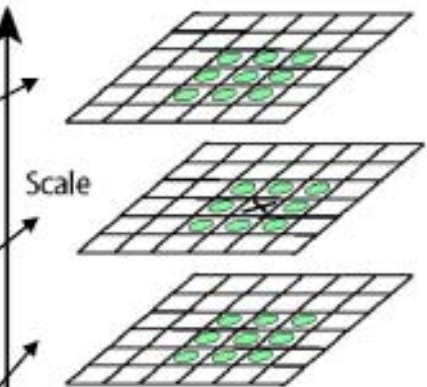
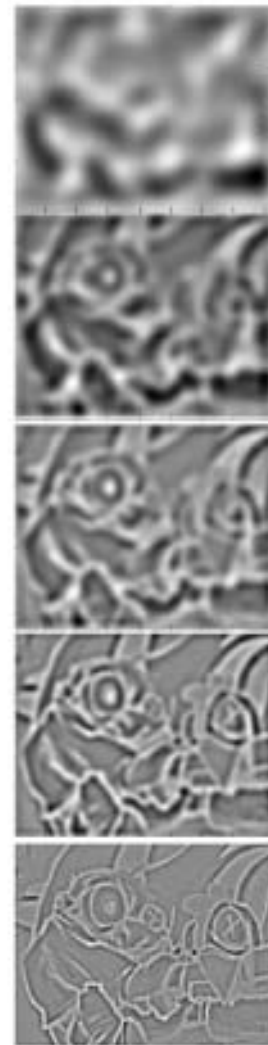
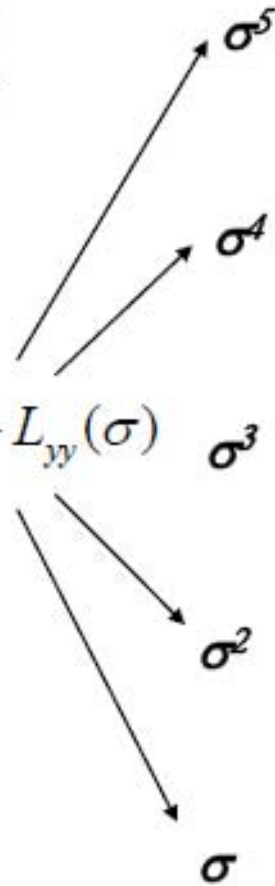
Slide adapted from Krystian Mikolajczyk

Laplacian-of-Gaussian (LoG)

- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

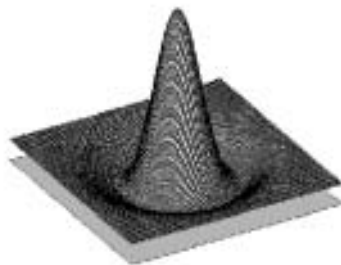


Slide adapted from

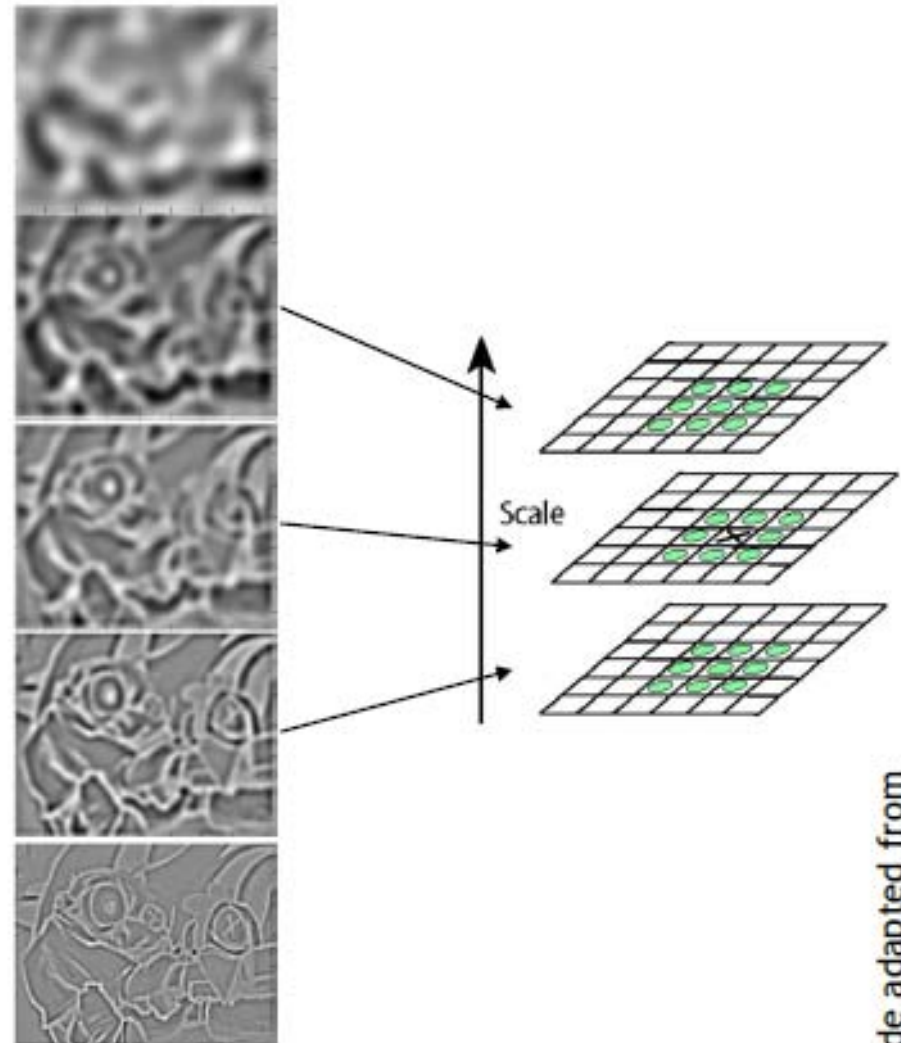
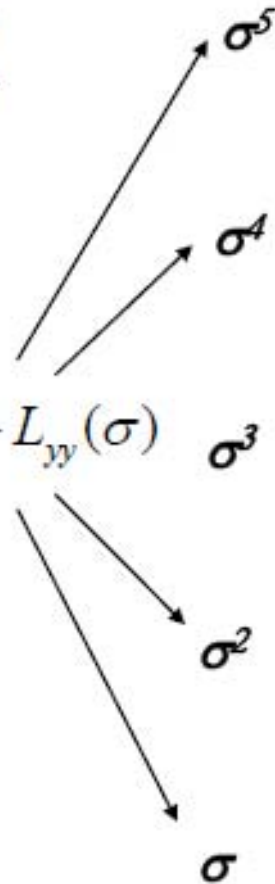


Laplacian-of-Gaussian (LoG)

- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



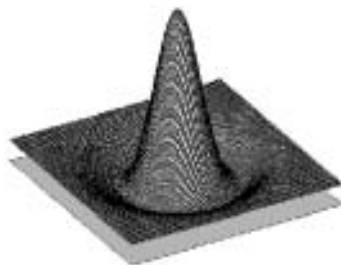
$$L_{xx}(\sigma) + L_{yy}(\sigma)$$



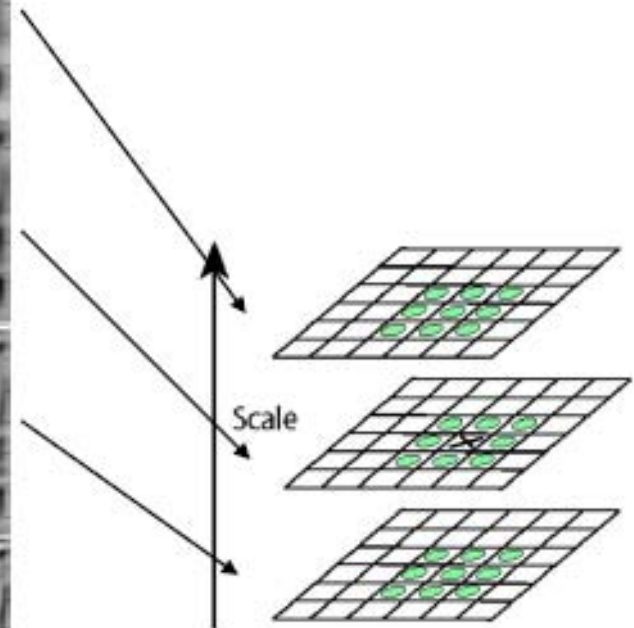
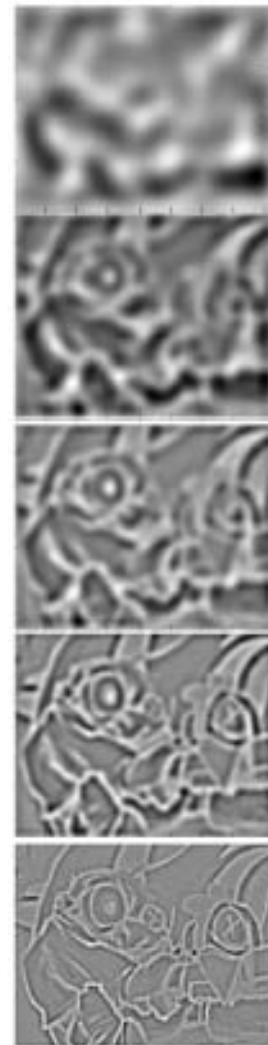
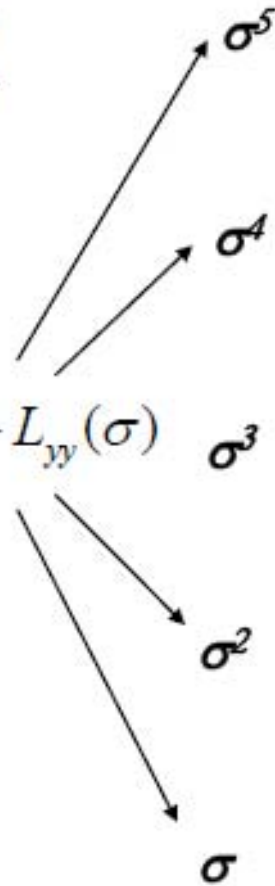
Slide adapted from

Laplacian-of-Gaussian (LoG)

- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma)$$



⇒ List of (x, y, σ)

Slide adapted from

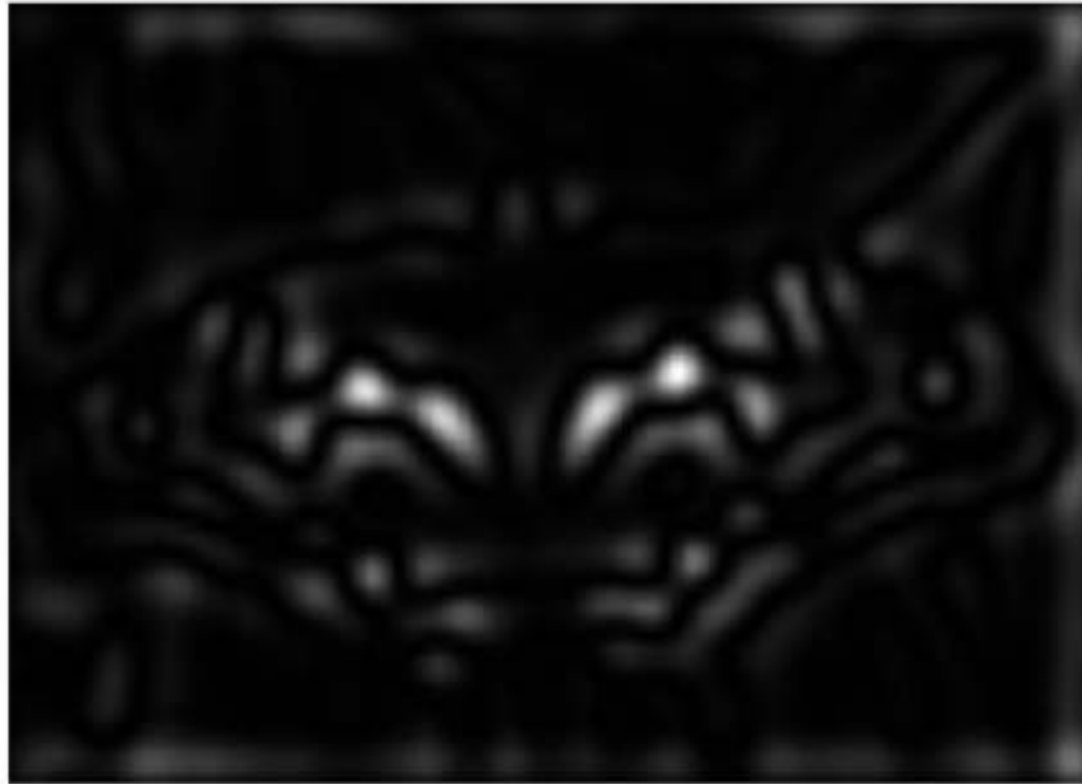
LoG Detector: Workflow



Slide credit: Svetlana Lazebnik



LoG Detector: Workflow

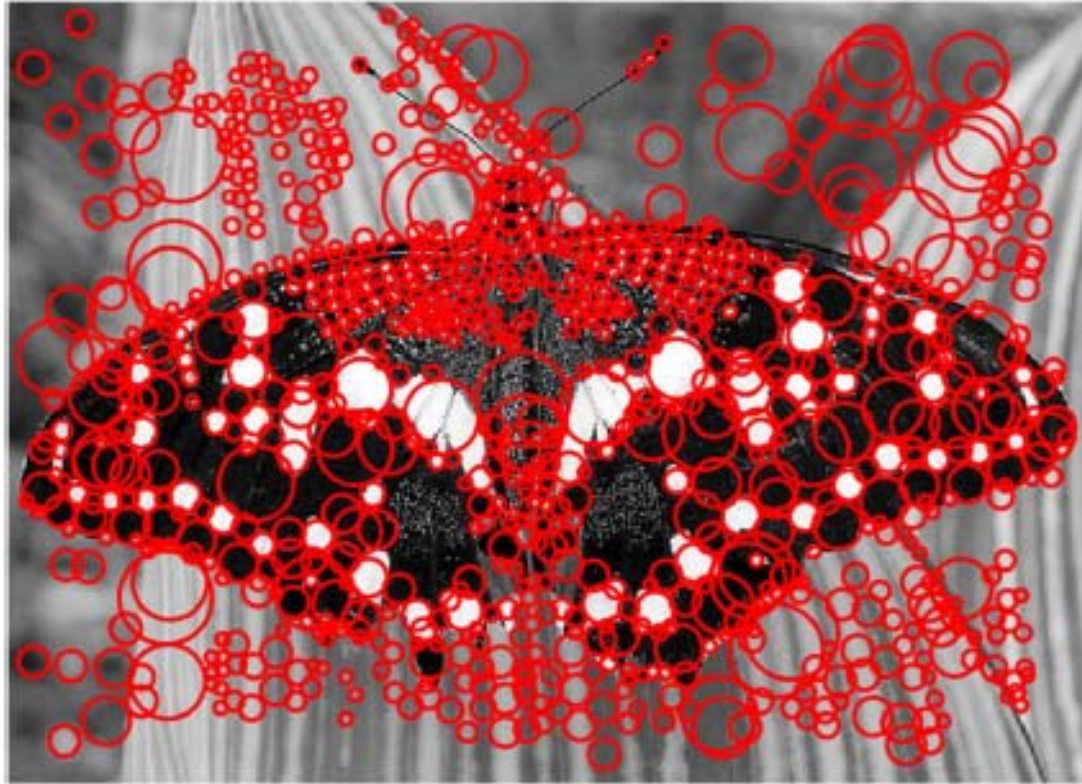


sigma = 11.9912

Slide credit: Svetlana Lazebnik



LoG Detector: Workflow



Slide credit: Svetlana Lazebnik

Technical Detail

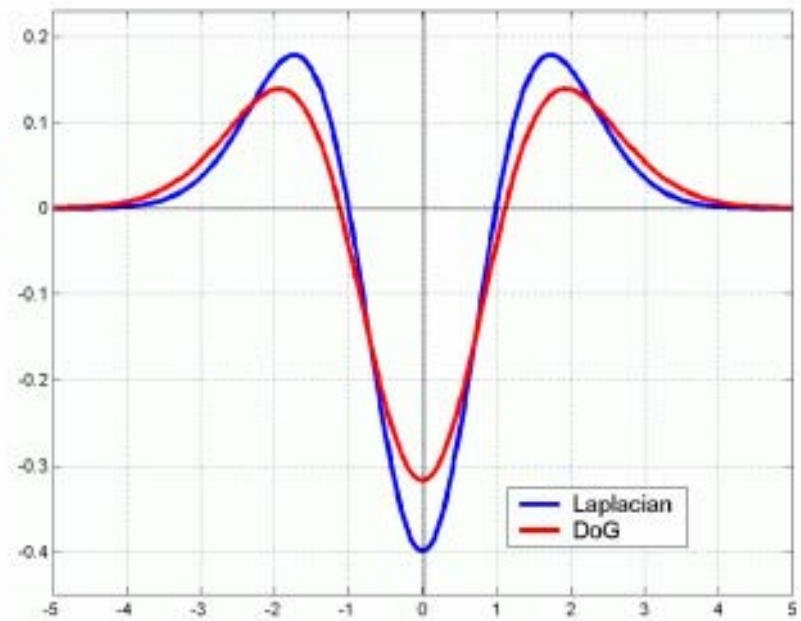
- We can efficiently approximate the Laplacian with a difference of Gaussians:

$$L = \sigma^2 (G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma))$$

(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

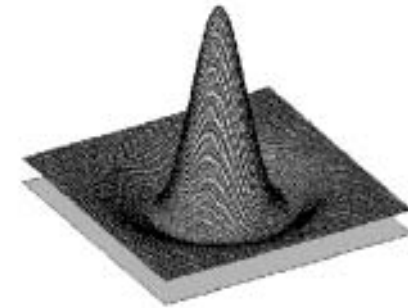
(Difference of Gaussians)



Slide credit: Bastian Leibe

Difference-of-Gaussian (DoG)

- Difference of Gaussians as approximation of the LoG
 - This is used e.g. in Lowe's SIFT pipeline for feature detection.
- Advantages
 - No need to compute 2nd derivatives
 - Gaussians are computed anyway, e.g. in a Gaussian pyramid.



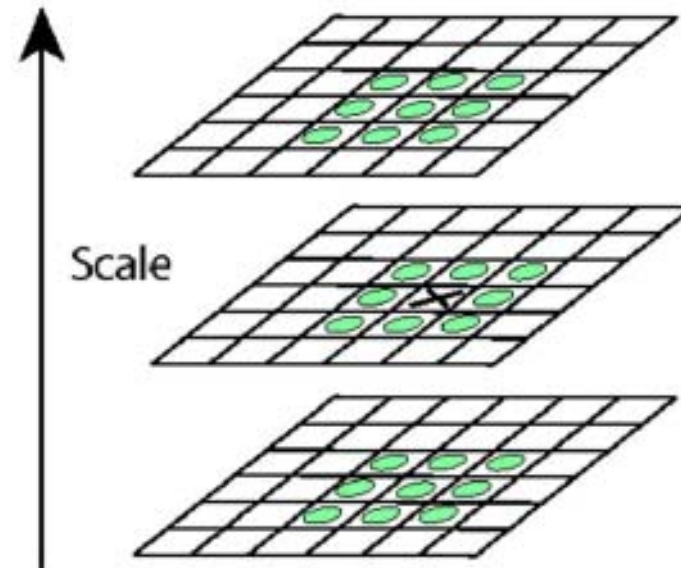
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Slide credit: Bastian Leibe

Key point localization with DoG

- Detect maxima of difference-of-Gaussian (DoG) in scale space
- Then reject points with low contrast (threshold)
- Eliminate edge responses

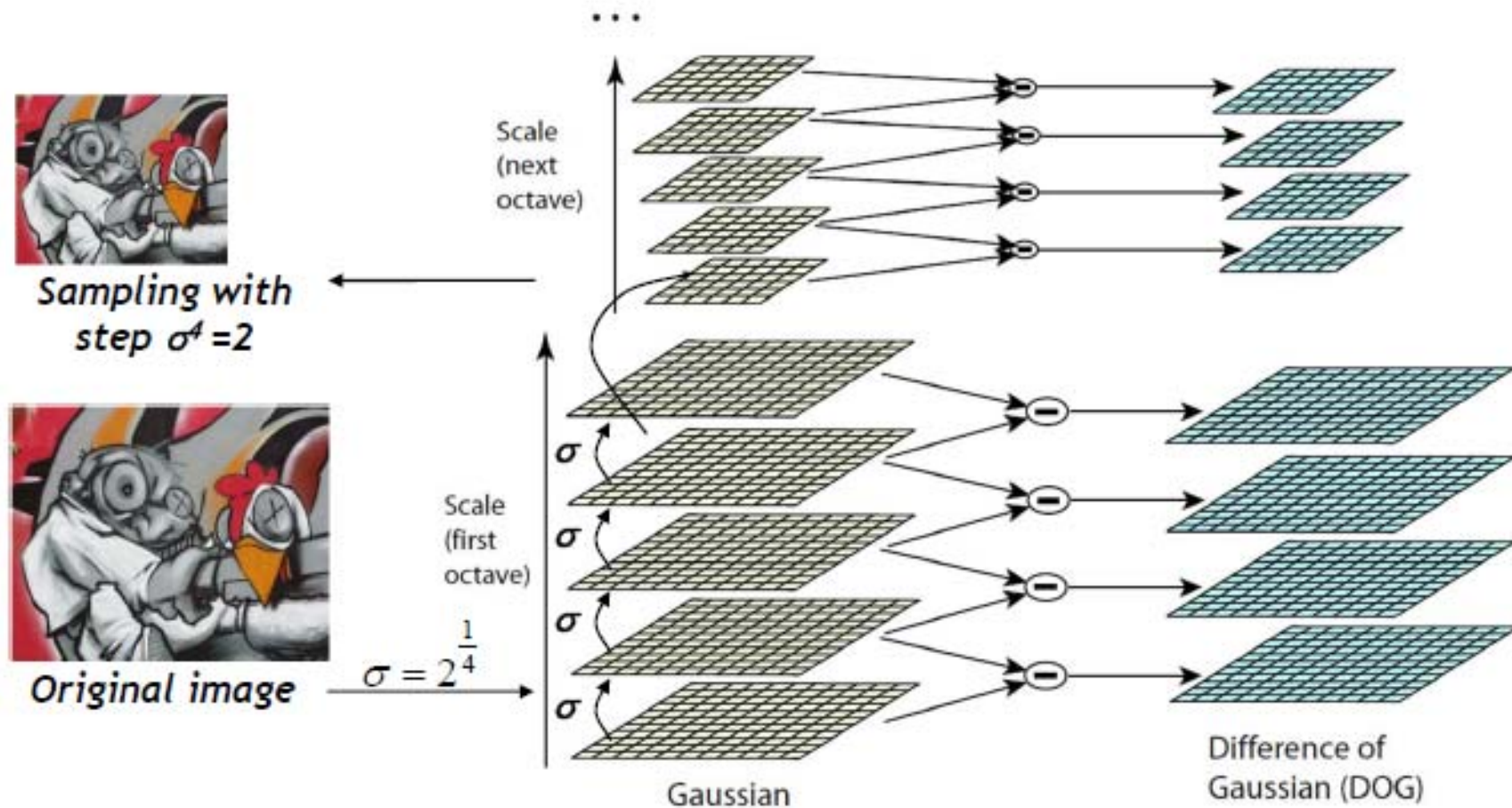


↓
Candidate keypoints:
list of (x, y, σ)

Slide credit: David Lowe

DoG – Efficient Computation

- Computation in Gaussian scale pyramid



Slide adapted from Krystian Mikolajczyk



Results: Lowe's DoG



Slide credit: Bastian Leibe

Example of Keypoint Detection



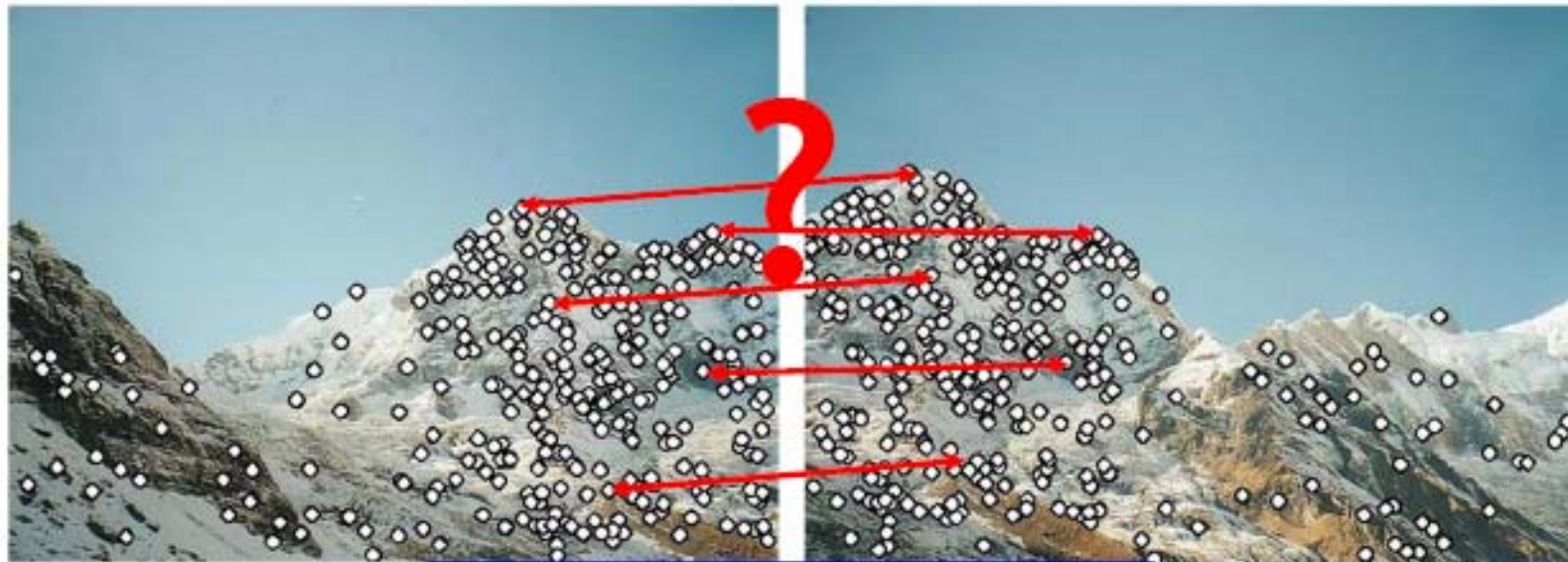
- (a) 233x189 image
- (b) 832 DoG extrema
- (c) 729 left after peak value threshold
- (d) 536 left after testing ratio of principle curvatures (removing edge responses)

Slide credit: David Lowe

Local Descriptors

- We know how to detect points
- Next question:

How to describe them for matching?



Point descriptor should be:

1. Invariant
2. Distinctive

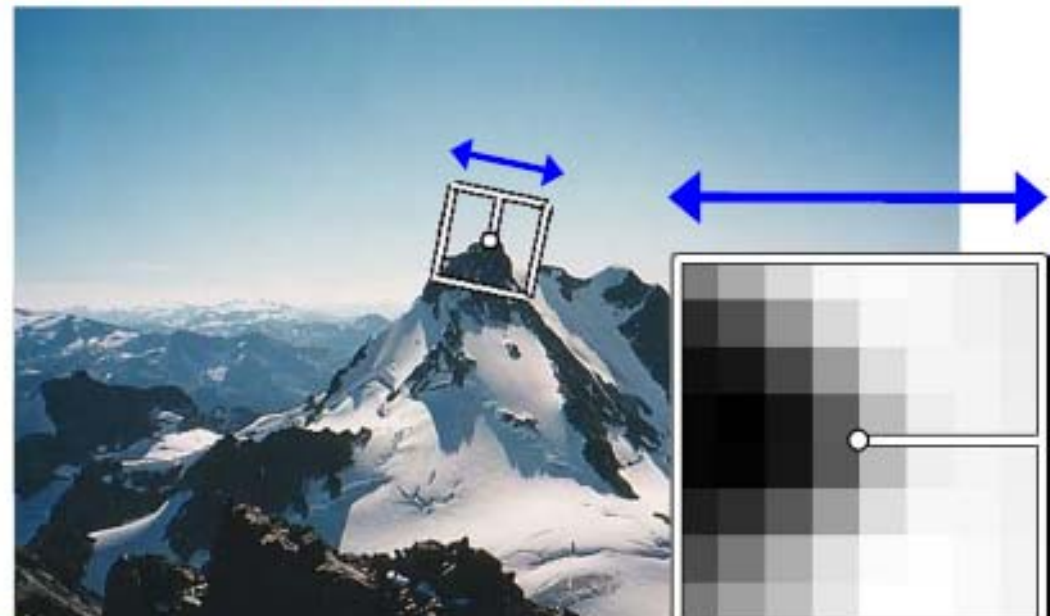
Slide credit: Kristen Grauman

Rotation Invariant Descriptors

- Find local orientation
 - Dominant direction of gradient for the image patch



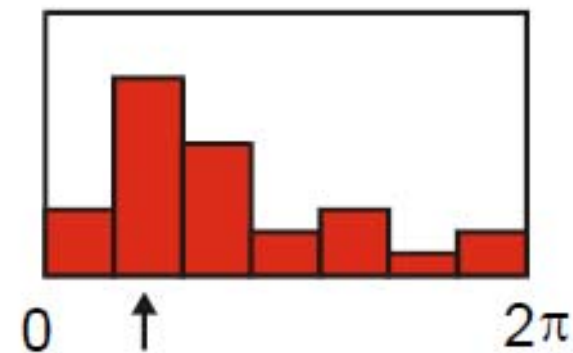
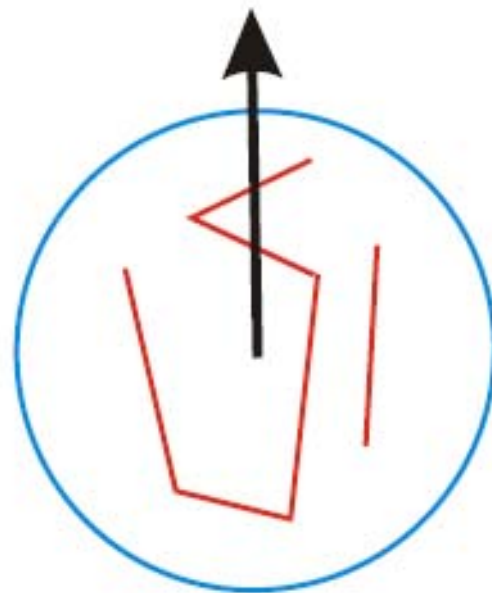
- Rotate patch according to this angle
 - This puts the patches into a canonical orientation.



Orientation Normalization: Computation

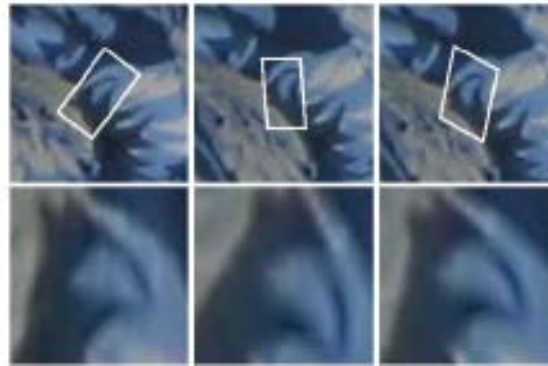
[Lowe, SIFT, 1999]

- Compute orientation histogram
- Select dominant orientation
- Normalize: rotate to fixed orientation

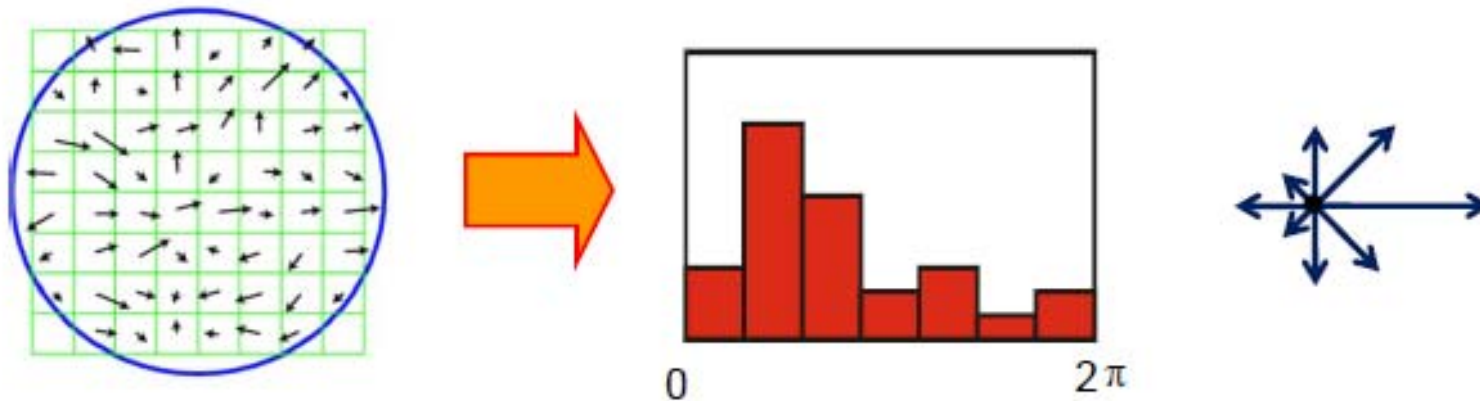


Feature Descriptors

- Disadvantage of patches as descriptors:
 - Small shifts can affect matching score a lot

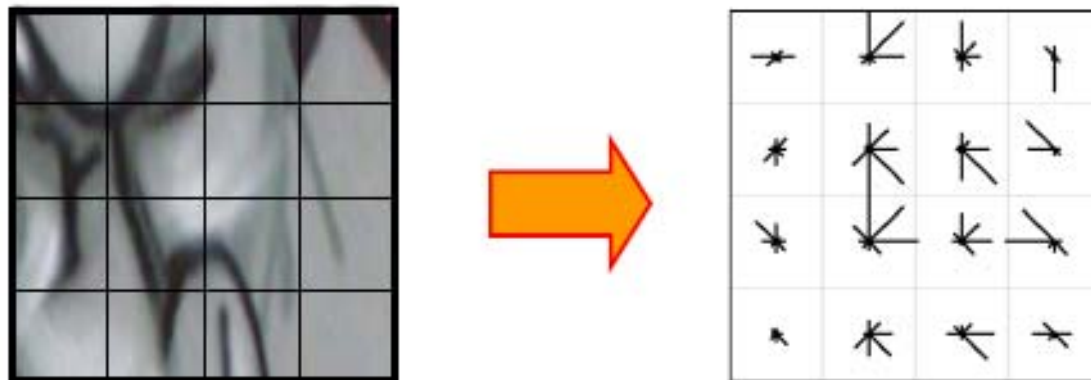


- Solution: histograms



Feature Descriptors: SIFT

- Scale Invariant Feature Transform
- Descriptor computation:
 - Divide patch into 4x4 sub-patches: 16 cells
 - Compute histogram of gradient orientations (8 reference angles) for all pixels inside each sub-patch
 - Resulting descriptor: $4 \times 4 \times 8 = 128$ dimensions



David G. Lowe. ["Distinctive image features from scale-invariant keypoints."](#) *IJCV* 60 (2), pp. 91-110, 2004.

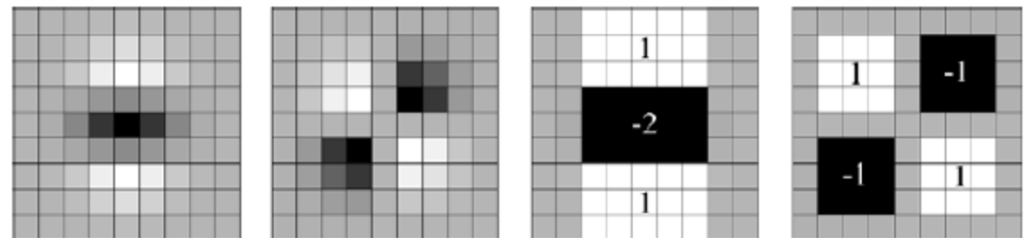
Overview: SIFT

- Extraordinarily robust matching technique
 - Can handle changes in viewpoint up to ~ 60 deg. out-of-plane rotation
 - Can handle significant changes in illumination
 - Sometimes even day vs. night (below)
 - Fast and efficient—can run in real time
 - Lots of code available
 - http://people.csail.mit.edu/albert/ladypack/wiki/index.php/Known_implementations_of_SIFT



Other Descriptors

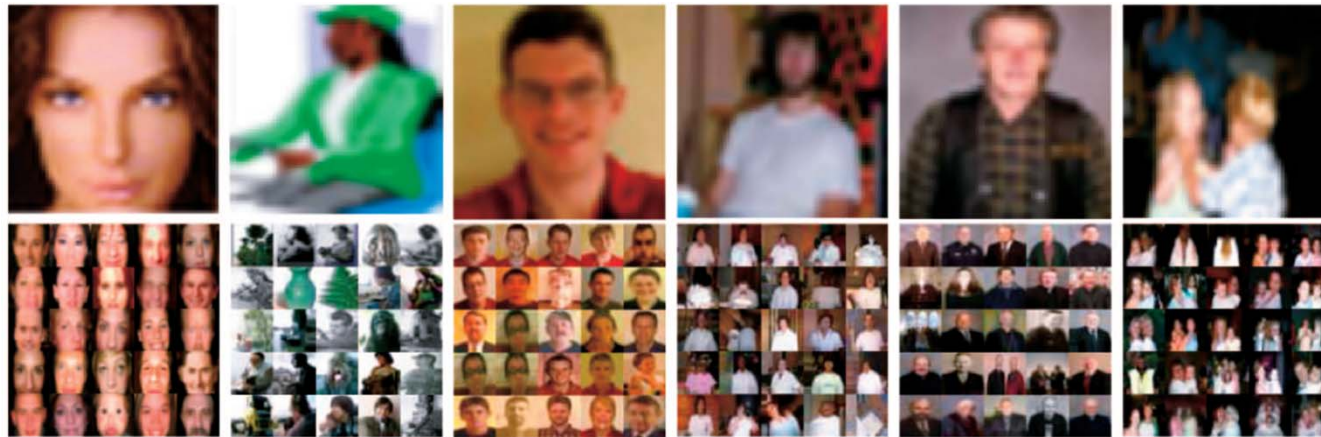
- **GIST: a kind of SIFT in a global scale**
- **SURF: an acceleration using the integral image, i.e., summed area table**



- **CNN features**

80M Tiny Images

- **Just use 32 by 32 images**
- **It works well even for recognition with a simple recognition method (nearest neighbor search) with using 80M data**



- **Indicates the importance of data**

PA1 (Optional)

- **Objective**
 - **Understand how to extract SIFT features and to use related libraries (OpenCV, vlfeat, ...)**



Class Objectives (Ch. 2.4) were:

- **Scale invariant region selection**
 - **Automatic scale selection**
 - **Laplacian of Gradients (LoG) \approx Difference of Gradients (DoG)**
 - **SIFT as a local descriptor**

Next Time...

- **Basic deep learning and its applications to computer vision**
- **Intro to object recognition**
- **Bag-of-Words (BoW) models**

Homework for Every Class

- **Go over the next lecture slides**
- **Come up with one question on what we have discussed today**
 - 1 for typical questions (that were answered in the class)
 - 2 for questions with thoughts or that surprised me
- **Write questions 3 times before the mid-term exam**
 - Write a question about one out of every four classes
 - Multiple questions in one time will be counted as one time
- **Common questions are compiled at [the Q&A file](#)**
 - Some of questions will be discussed in the class
- **If you want to know the answer of your question, ask me or TA [on person](#)**