

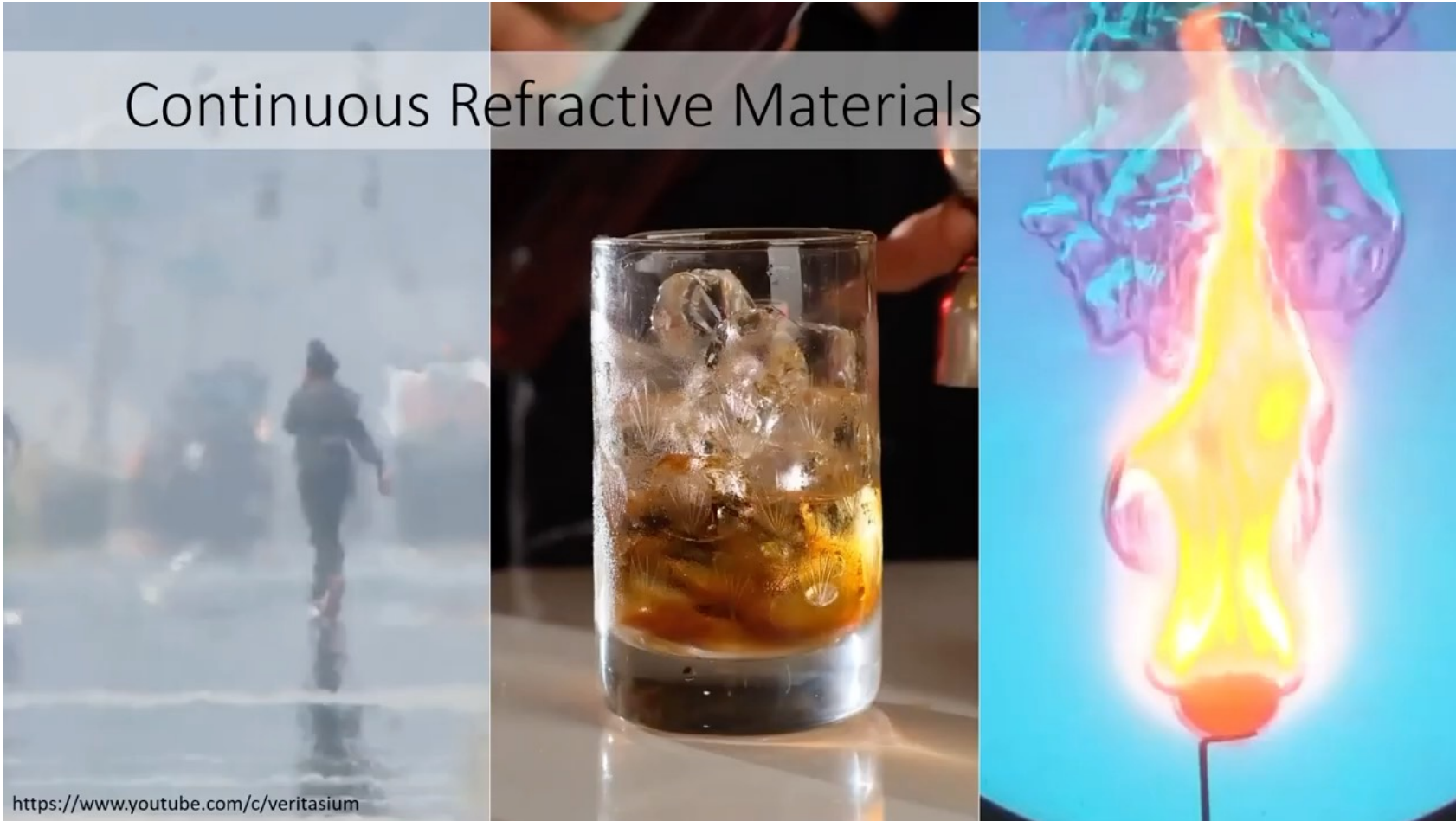
Final Presentation

ADJOINT NONLINEAR RAYTRACING

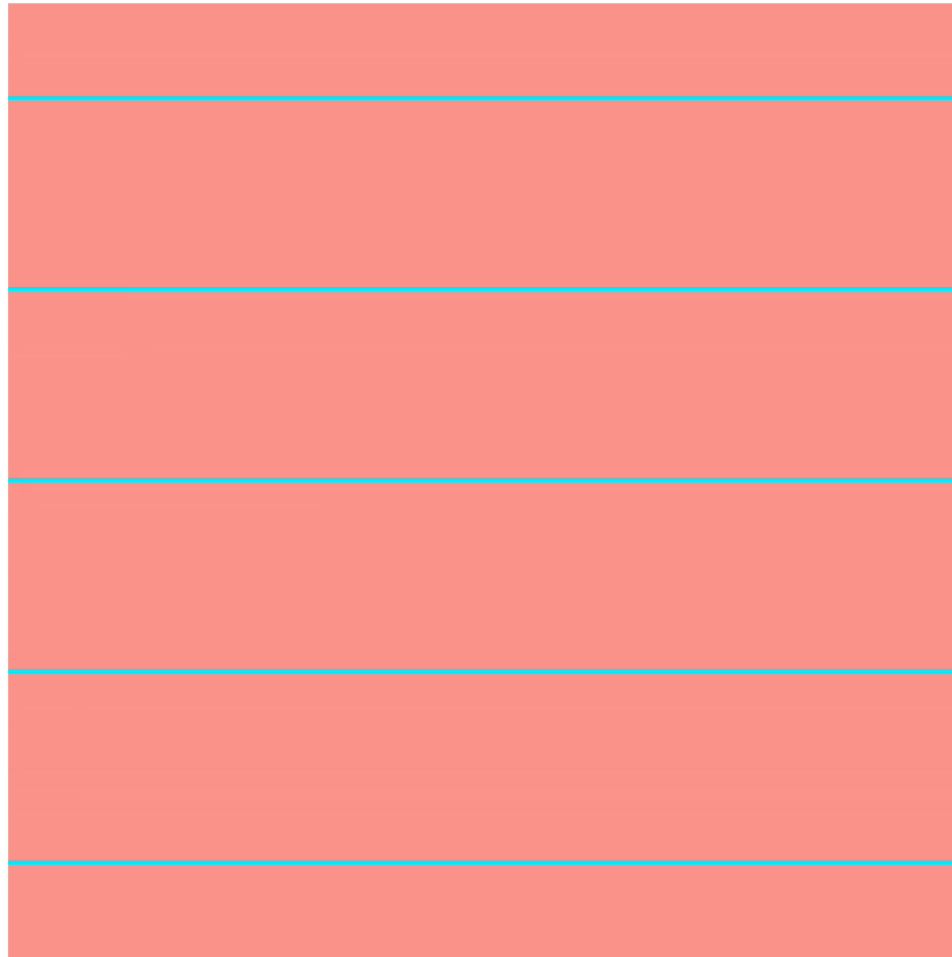
Jeong Uk Lee and Philipp Derr

Recap

Continuous Refractive Materials

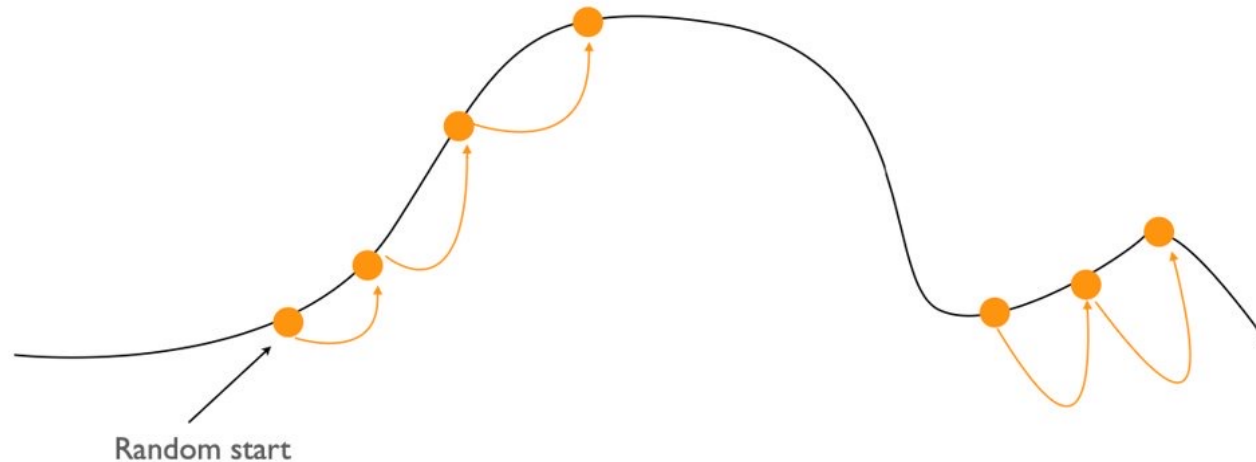


Recap



Problem #1

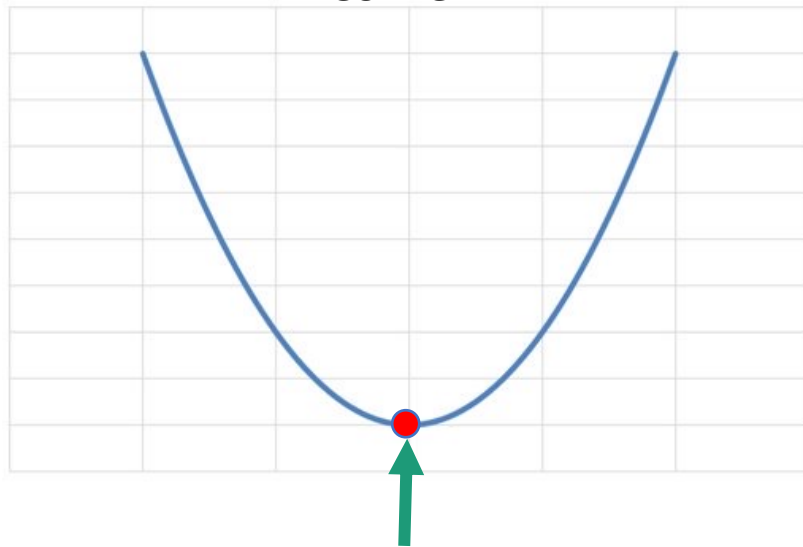
- Gradient-based optimization procedure requires a good **initialization**.
- Start from **randomly distributed** spatially varying medium.



Problem #1

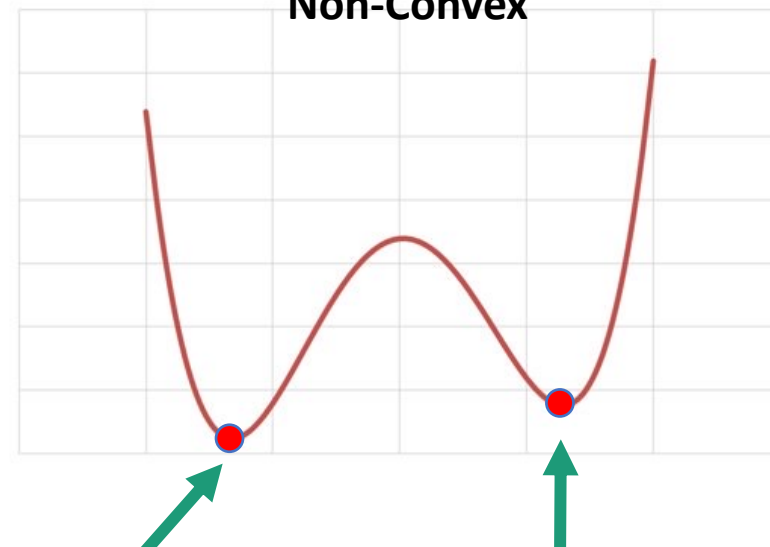
- Current method initializes a uniform **refractive index** of **1**.
- Can lead to wrong solution in non-convex cases.
- optimization landscape is highly non-convex

Convex



Global Minima(ok)

Non-Convex



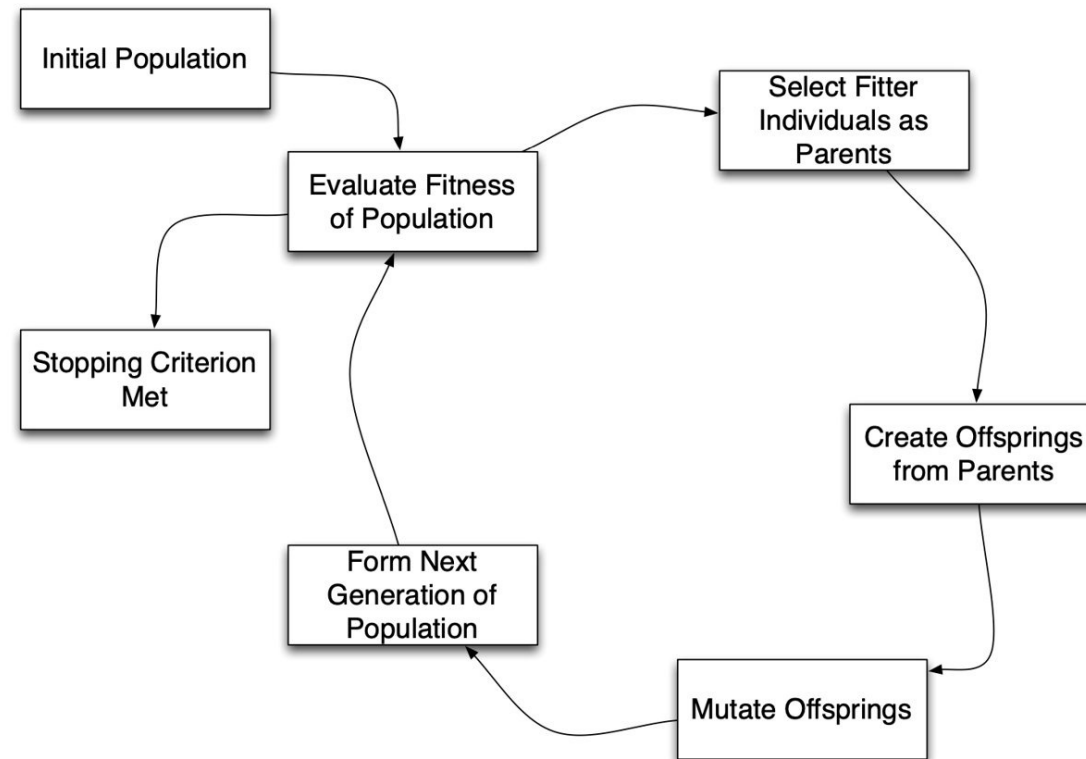
Global Minima

Local minima(wrong)

Problem #1

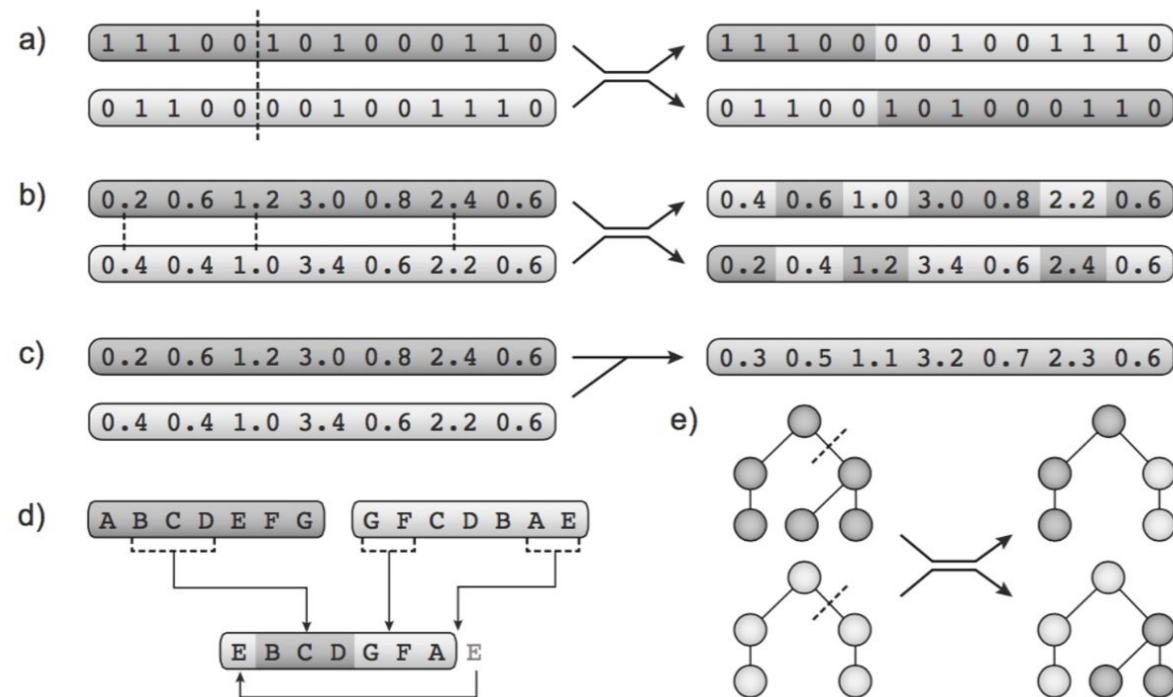
- Find better Initialization process
- gradient-based optimization procedure requires a good initialization
- **Paper implementation:**
 - initializing to a uniform refractive index field gave satisfactory results. $\eta(x) = 1$
 - To ensure that the recovered reconstruction is physically plausible, after every gradient descent iteration, we project η to be greater than or equal to 1 (projected gradient descent).

Problem #1



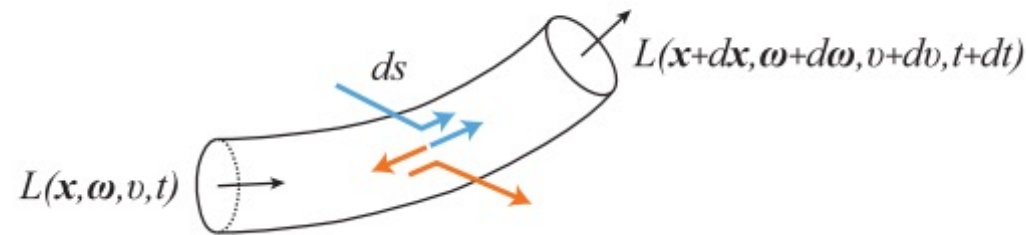
Problem #1

Crossover Operators



Problem #2

- Specifically apply to media where there is only continuous refraction and no volumetric scattering.
- The radiance varies through medium because of **in-scattering(blue)** and **out-scattering(red)**.



Ament, Marco, Christoph Bergmann, and Daniel Weiskopf. "Refractive radiative transfer equation." *ACM Transactions on Graphics (TOG)* 33.2 (2014): 1-22.

Problem #2

- The paper introduces **Refractive Radiative Transfer Equation(RRTE)**.
- Estimation of basic radiance using photon mapping.

$$\tilde{L}_i(\mathbf{x}, \boldsymbol{\omega}, \nu, t) = \frac{\Lambda}{4\pi} \int_{\Omega} \tilde{L}(\mathbf{x}, \boldsymbol{\omega}_i, \nu, t) P(\boldsymbol{\omega}_i, \boldsymbol{\omega}) d\boldsymbol{\omega}_i \quad (34)$$

$$= \frac{\Lambda}{4\pi n^2} \int_{\Omega} \nu_g h\nu f P(\boldsymbol{\omega}_i, \boldsymbol{\omega}) d\boldsymbol{\omega}_i \quad (35)$$

$$= \frac{\Lambda}{4\pi n^2} \int_{\Omega} \frac{h\nu}{\sigma_s} \nu_g \sigma_s f P(\boldsymbol{\omega}_i, \boldsymbol{\omega}) d\boldsymbol{\omega}_i \quad (36)$$

$$= \frac{\Lambda}{4\pi n^2} \int_{\Omega} \frac{1}{\sigma_s} \frac{d^4 W}{dx d\boldsymbol{\omega}_i d\nu dt} P(\boldsymbol{\omega}_i, \boldsymbol{\omega}) d\boldsymbol{\omega}_i \quad (37)$$

$$= \frac{\Lambda}{4\pi n^2} \int_{\Omega} \frac{1}{\sigma_s} \frac{d^3 \Phi}{dx d\boldsymbol{\omega}_i d\nu} P(\boldsymbol{\omega}_i, \boldsymbol{\omega}) d\boldsymbol{\omega}_i \quad (38)$$

$$= \frac{\Lambda}{4\pi n^2} \int_{\Omega} L(\mathbf{x}, \boldsymbol{\omega}_i, \nu, t) P(\boldsymbol{\omega}_i, \boldsymbol{\omega}) d\boldsymbol{\omega}_i \quad (39)$$

$$=: \frac{1}{n^2} L_i(\mathbf{x}, \boldsymbol{\omega}_i, \nu, t). \quad (40)$$

Ament, Marco, Christoph Bergmann, and Daniel Weiskopf. "Refractive radiative transfer equation." *ACM Transactions on Graphics (TOG)* 33.2 (2014): 1-22.

Original Idea

- Random Search
- Genetic Algorithms:
 1. Start with a random population of refractive index field
 2. Evaluate them give each one a score(fitness)
 3. Select different field and recombine to get new field(offspring)
 4. Random mutation
 5. Evaluate new population
 6. Start from 2. again
- Refractive Radiative Transfer Equation:
 1. Start the refraction optimization process.
 2. Introduce scattering by measuring radiance for each step.

Expected Results

- **Benefits**

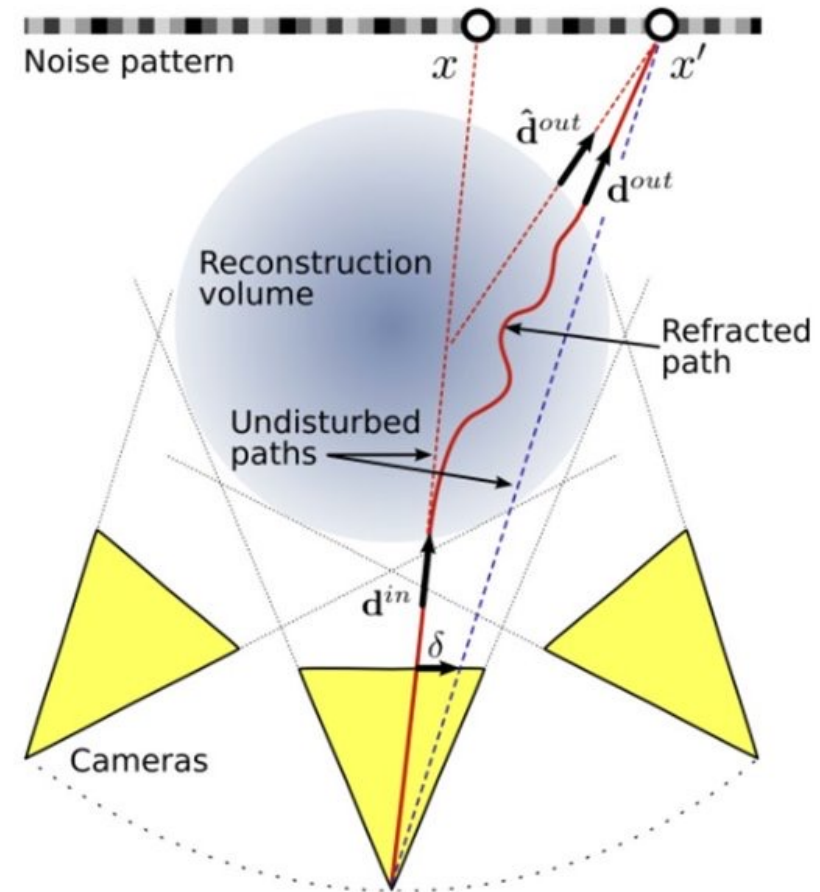
- Faster convergence(i.e. less steps)
- Will get stuck less in local optima
- Can get a common refractive index field for different lenses and gas
- Make ray behavior more realistic by introducing scattering.

- **Drawback**

- Each step takes long time.
- Not sure if result will be satisfactory
- Refractive field can be hyper optimized for one lens(overfitting)

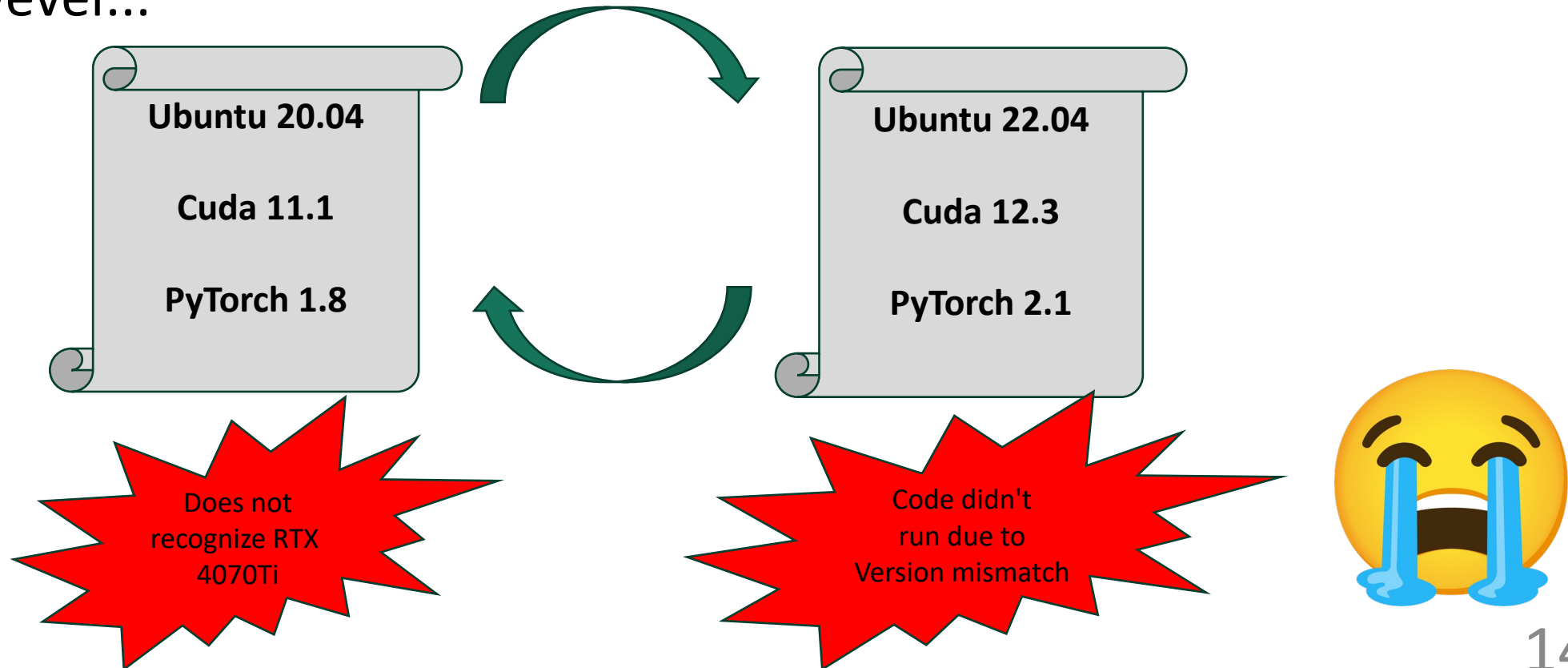
Other Methods

- Time-resolved 3D Capture of Non-stationary Gas Flows – SIGGRAPH Asia 2008
- reconstructions from techniques assuming a single refraction event
- Allows to make an approximation
- Background Oriented Schlieren BOS



Project failure...

- **Plan:** Make contribution to the existing code.
- However...



Roles

- **Jeong Uk Lee:**

- Project setup
- Scattering implementation

- **Philipp Derr:**

- Finding possible solutions for problems.
- GA Implementation

Source

- Teh, Arjun, Matthew O'Toole, and Ioannis Gkioulekas. "Adjoint nonlinear ray tracing." ACM Transactions on Graphics (TOG) 41.4 (2022): 1-13.
- CS454 AI Based Software Engineering: Shin Yoo
- <https://www.cs.ubc.ca/labs/imager/tr/2008/GasCapture/gascapture.pdf>
- Ament, Marco, Christoph Bergmann, and Daniel Weiskopf. "Refractive radiative transfer equation." ACM Transactions on Graphics (TOG) 33.2 (2014): 1-22.