CS482: Monte Carlo Ray Tracing:

Sung-Eui Yoon (윤성의)

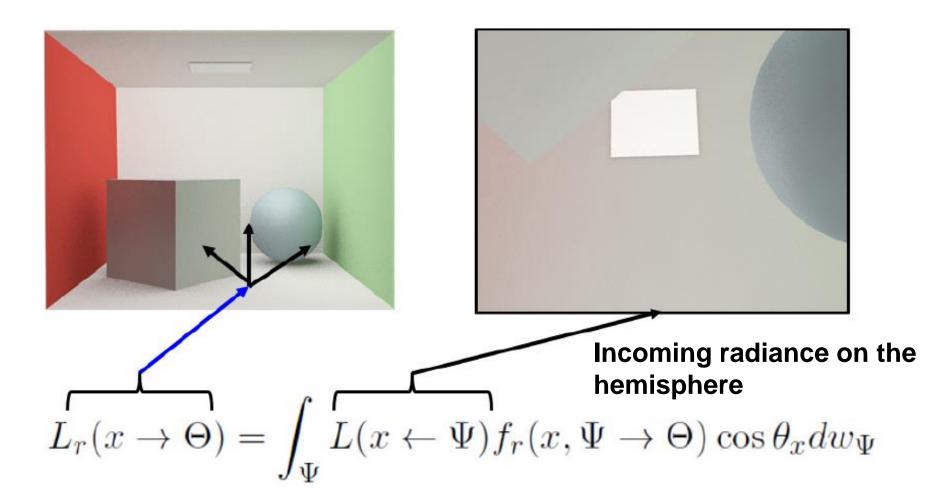
http://sglab.kaist.ac.kr/~sungeui/IC?

Class Objectives (Ch. 15)

- Understand a basic structure of Monte Carlo ray tracing
 - Russian roulette for its termination
 - Path tracing
- Last time:
 - Monte Carlo integration: sampling approach for solving the rendering equation
 - Estimator and its variance



Rendering Equation

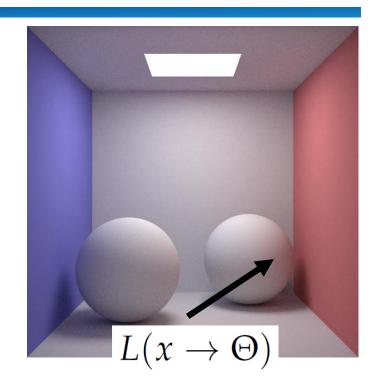




Evaluation

- To compute $L(x \to \Theta)$:
 - Check $L_e(x \to \Theta)$

• Evaluate $L_r(x \to \Theta)$



$$L_r(x \to \Theta) = \int_{\Psi} L(x \leftarrow \Psi) f_r(x, \Psi \to \Theta) \cos \theta_x dw_{\Psi}$$



Evaluation

- Use Monte Carlo
- Generate random directions on hemisphere Ψ using pdf p(Ψ)

$$L_r(x \to \Theta) = \int_{\Psi} L(x \leftarrow \Psi) f_r(x, \Psi \to \Theta) \cos \theta_x dw_{\Psi}$$

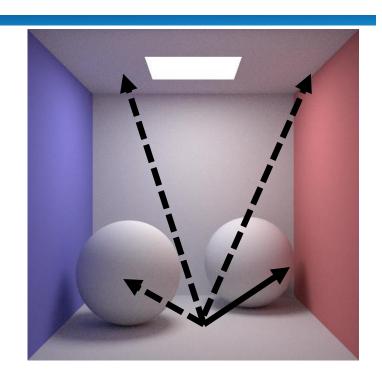
$$\hat{L}_r(x \to \Theta) = \frac{1}{N} \sum_{i=1}^{N} \frac{L(x \leftarrow \Psi_i) f_r(x, \Psi_i \to \Theta) \cos \theta_x}{p(\Psi_i)}$$

• How about $L(x \leftarrow \Psi_i)$?



Evaluation

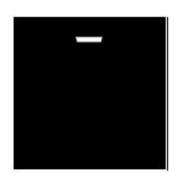
- How about $L(x \leftarrow \Psi_i)$?
- Perform ray casting backward
- Compute radiance from those visible points to x
 - Assume reciprocity



- Recursively perform the process
 - Each additional bounce supports one more indirect illumination



When to end recursion?









From kavita's slides

- Contributions of further light bounces become less significant
 - Max recursion
 - Some threshold for radiance value
- If we just ignore them, estimators will be biased



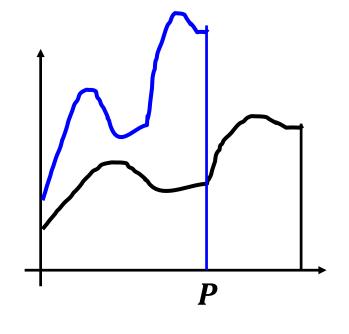
Russian Roulette

• Integral: Substitute y = Px

$$I = \int_0^1 f(x) dx = \int_0^P \frac{f(y/P)}{P} dy.$$

Estimator

$$\hat{I}_{roulette} = \begin{cases} \frac{f(x_i)}{P} & \text{if } x_i \leq P, \\ 0 & \text{if } x_i > P. \end{cases}$$



• Variance?



Russian Roulette

- Pick absorption probability, a = 1-P
 - Recursion is terminated
- 1- a, i.e., P, is commonly to be equal to the reflectance of the material of the surface
 - Darker surface absorbs more paths



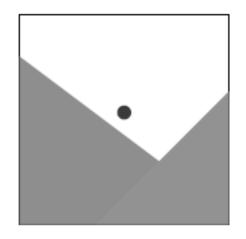
Algorithm so far

- Shoot primary rays through each pixel
- Shoot indirect rays, sampled over hemisphere
- Terminate recursion using Russian Roulette



Pixel Anti-Aliasing

- Compute radiance only at the center of pixel
 - Produce jaggies



- We want to evaluate using MC
- Simple box filter
 - The averaging method



Stochastic Ray Tracing

- Parameters
 - Num. of starting ray per pixel

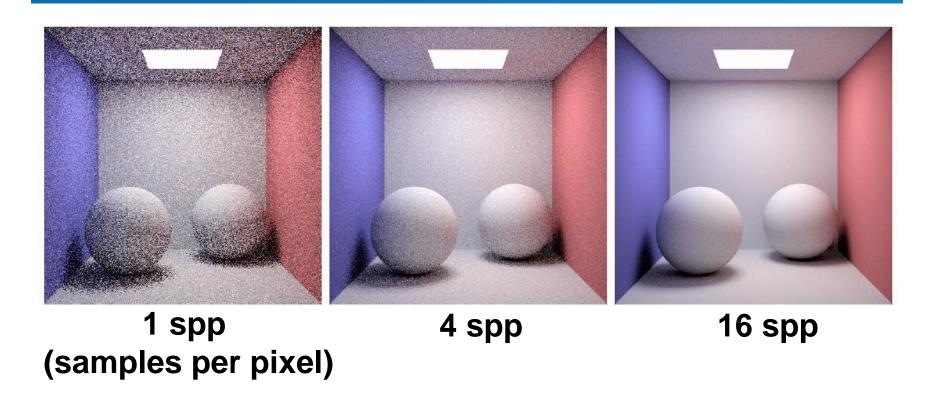
• Num. of random rays for each surface point (branching factor)

Path tracing





Path Tracing



 Pixel sampling + light source sampling folded into one method



Algorithm so far

- Shoot primary rays through each pixel
- Shoot indirect rays, sampled over hemisphere
 - Path tracing shoots only 1 indirect ray
- Terminate recursion using Russian Roulette

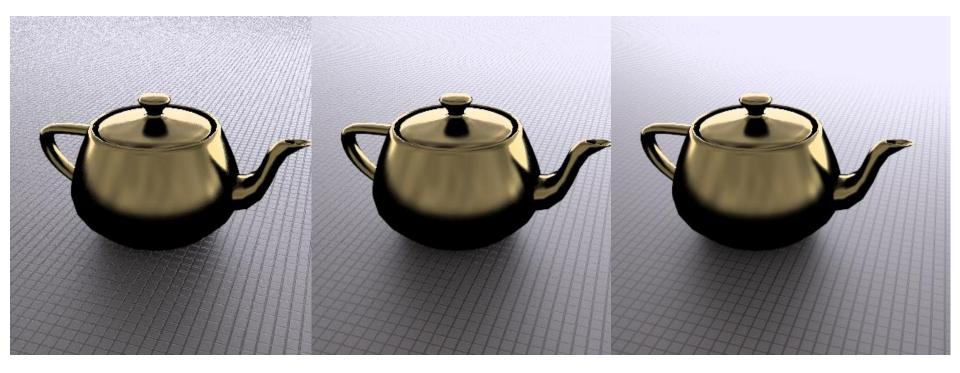


Performance

- Want better quality with smaller # of samples
 - Fewer samples/better performance
 - Quasi Monte Carlo: well-distributed samples
 - Adaptive sampling



Some Example



Uniform sampling (64 samples per pixel)

Adaptive sampling

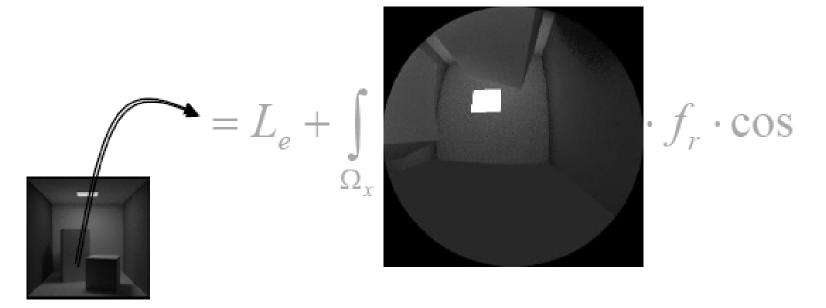
Reference



Importance Sampling

$$L(x \to \Theta) = L_{\varepsilon}(x \to \Theta) + \int_{\Omega_x} f_r(\Psi \leftrightarrow \Theta) \cdot L(x \leftarrow \Psi) \cdot \cos(\Psi, n_x) \cdot d\omega_{\Psi}$$

Radiance from light sources + radiance from other surfaces





Importance Sampling

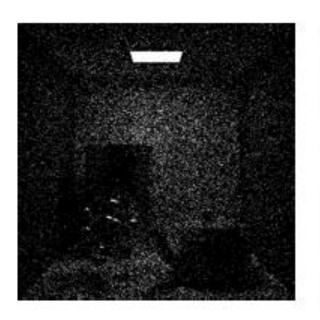
$$L(x \rightarrow \Theta) = L_e + L_{direct} + L_{indirect}$$

$$=L_e + \int_{\Omega_x} \mathbf{r} \cdot \mathbf{r} \cdot$$

 So ... sample direct and indirect with separate MC integration



Comparison





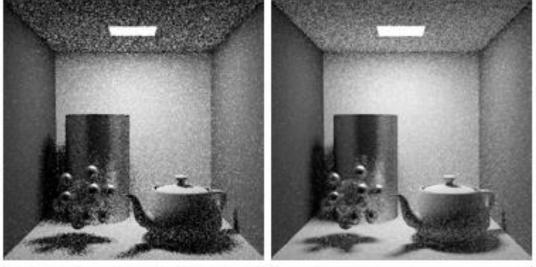
From kavita's slides

- With and without considering direct illumination
 - 16 samples / pixel



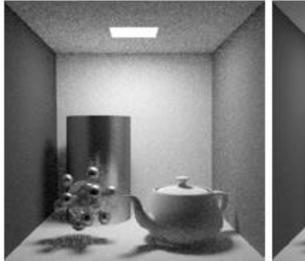
Rays per pixel

1 sample/ pixel



4 samples/ pixel

16 samples/ pixel



256 samples/ pixel



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Next Time...

Acceleration techniques for global illumination methods



Homework

- Go over the next lecture slides before the class
- Watch 2 SIG/CVPR/ISMAR videos and submit your summaries every Mon. class
 - Just one paragraph for each summary
 - Any top-tier conf (e.g., ICRA) is okay

Example:

Title: XXX XXXX XXXX

Abstract: this video is about accelerating the performance of ray tracing. To achieve its goal, they design a new technique for reordering rays, since by doing so, they can improve the ray coherence and thus improve the overall performance.